

Trustworthy Geometric Perception: Certifiable Optimization and Robust Estimation

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Best of ICRA Virtual Meetup



Universidad
Zaragoza

1474

1

Motivation: Why Trustworthy Perception?

2

Certifiable Global Optimization

- GlobustVP: Certifiable VP Estimation [CVPR 2025, Best Paper Award Candidate]
- NPC: RL-Accelerated Homotopy Solvers [ICLR 2026]
- Survey of Global Solvers for 3D Vision

3

Open challenges

1

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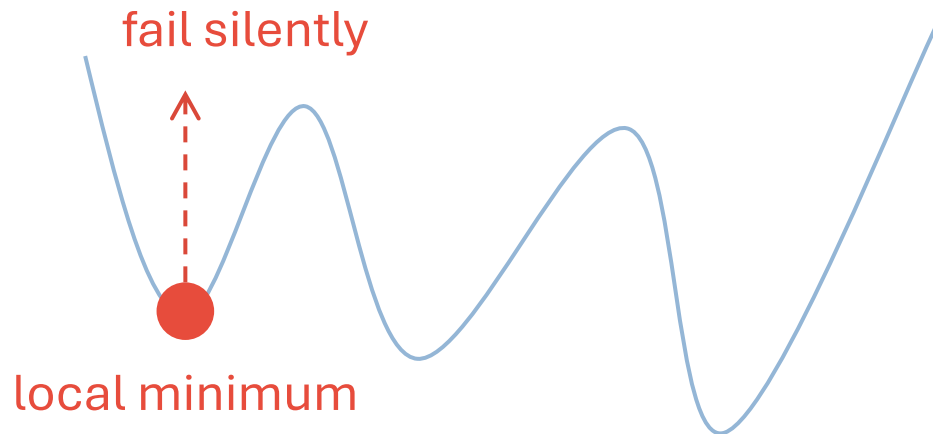
3

Open challenges

Motivation: Why Trustworthy Perception

Local Optimization

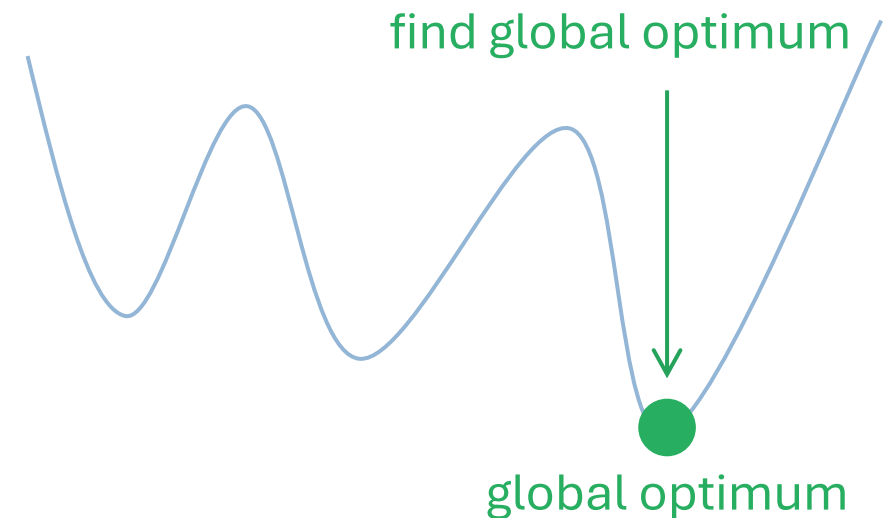
- ✗ Sensitive to initialization
- ✗ Fails silently, no warning when wrong
- ✗ No optimality guarantee



vs.

Certifiable Optimization

- ✓ Globally optimal solution
- ✓ Knows when it is correct
- ✓ Optimality certificate provided



Research Vision: Trustworthy Geometric Perception

Direction 1

Certifiable Global Optimization

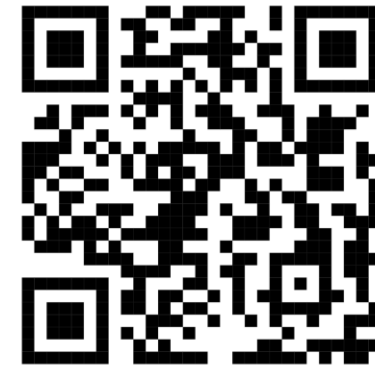
Convex relaxation (SDP/QCQP) and polynomial methods providing formal optimality guarantees

This talk!

Direction 2

Robust Estimation

Perception reliability under motion blur, dynamic scenes, and featureless environments



1

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Open challenges

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Certifiable Global Optimization

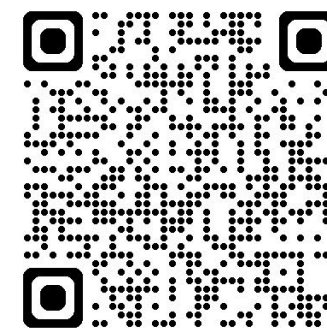
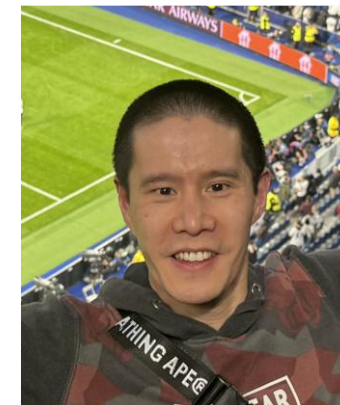
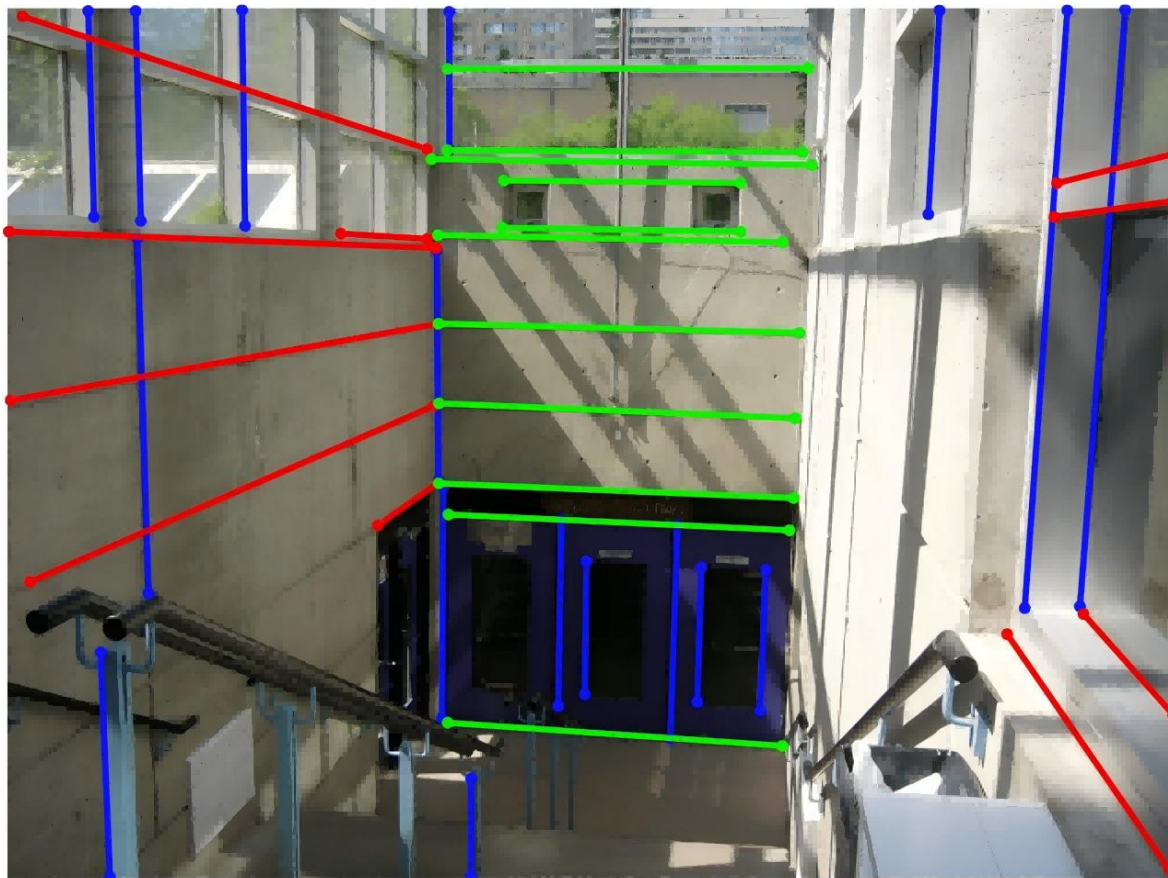
- GlobustVP: Certifiable VP Estimation [CVPR 2025, Best Paper Award Candidate]
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3

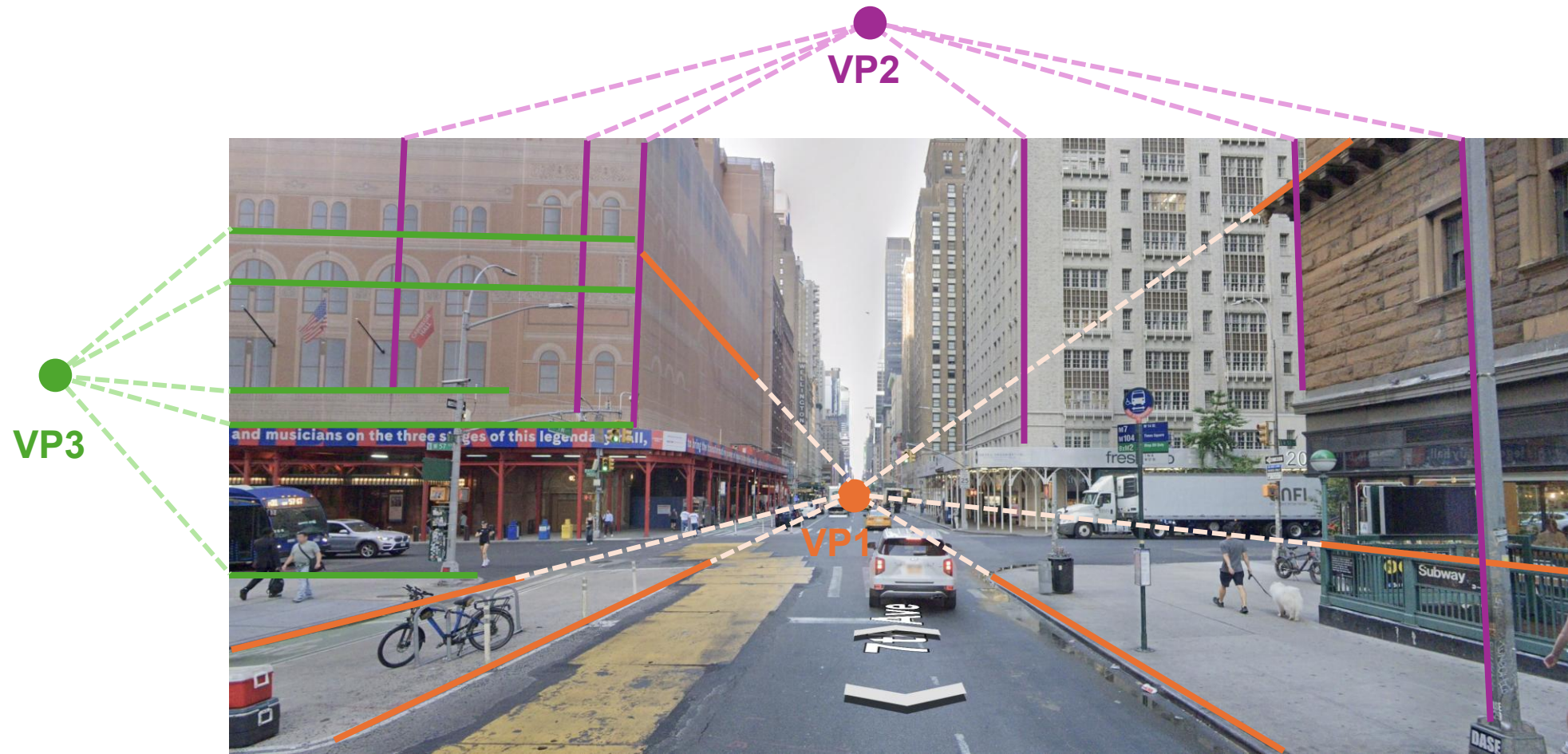
Open challenges

GlobustVP:

Convex Relaxation for Robust Vanishing Point Estimation in Manhattan World



Vanishing Point in Manhattan World



Applications of Vanishing Point

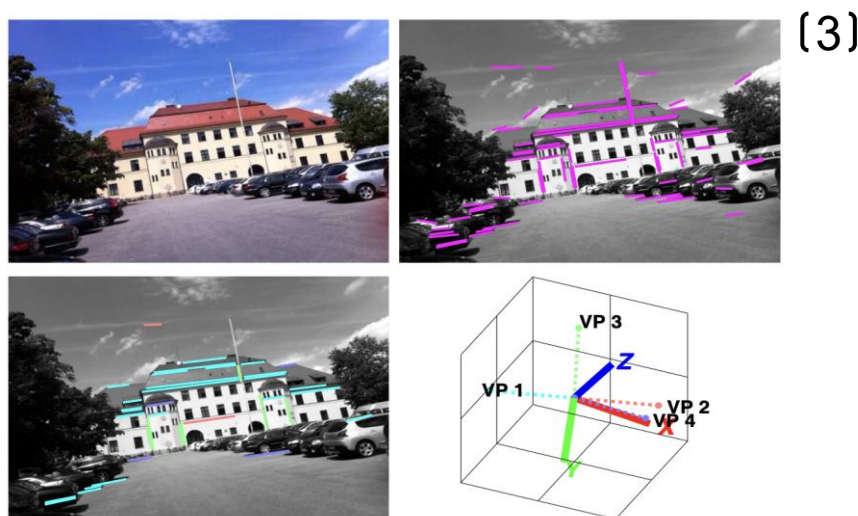
Structure from Motion (SFM)



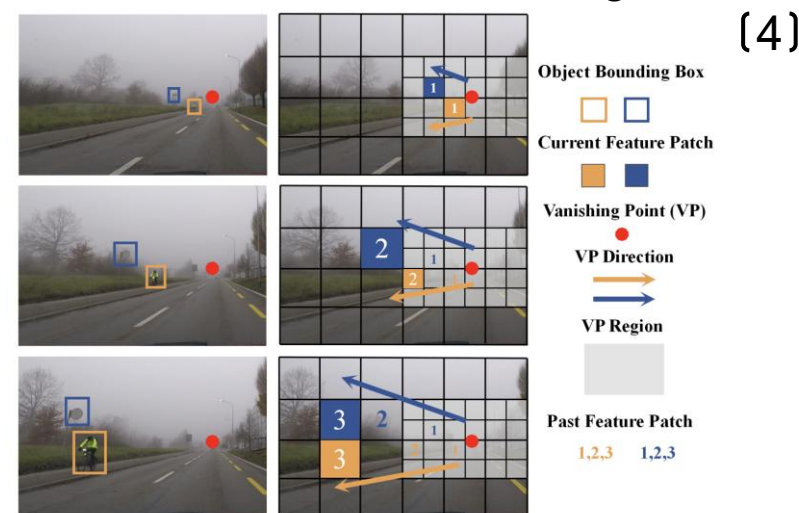
Simultaneous Localization And Mapping (SLAM)



Camera Rotation Estimation



Structural Understanding



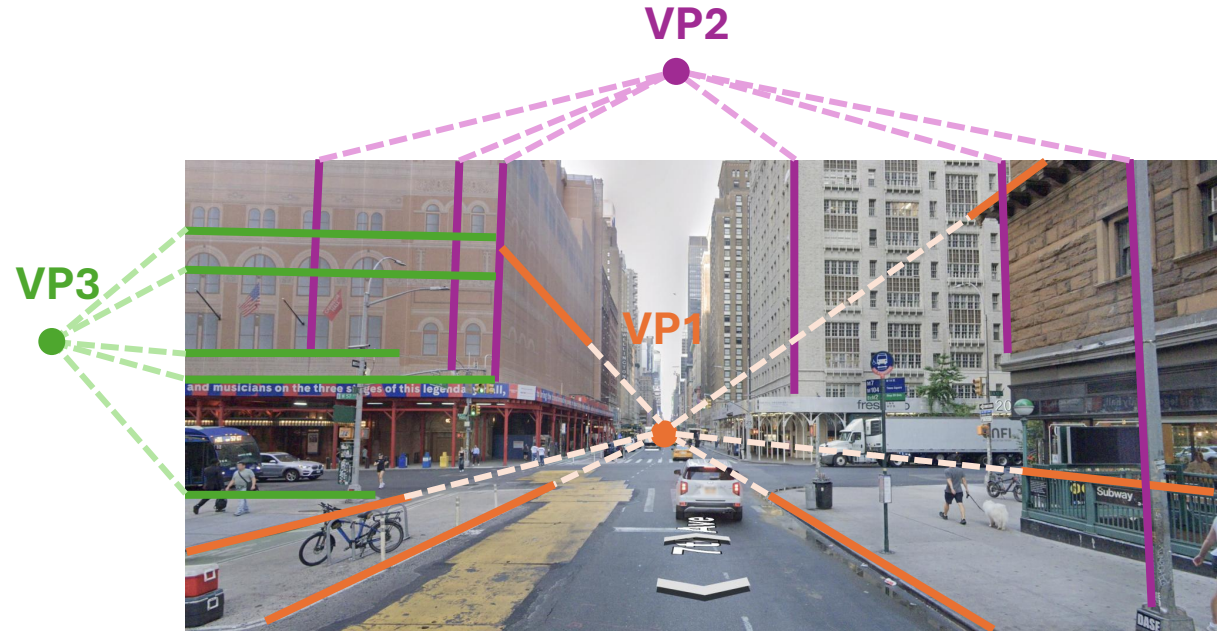
[1] Liu S, Yu Y, Pautrat R, et al. 3d line mapping revisited. CVPR 2023.

[2] Li Y, Yunus R, Brasch N, et al. RGB-D SLAM with structural regularities. ICRA 2021.

[3] Lee J K, Yoon K J. Real-time joint estimation of camera orientation and vanishing points. CVPR 2015.

[4] Guo D, Fan D P, Lu T, et al. Vanishing-point-guided video semantic segmentation of driving scenes. CVPR 2024.

Problem: VPs Estimation & Line Labeling



Input: Unlabeled Lines
Intrinsic Parameters



Output: Labeled Lines
Vanishing Points (VP)



**Global
Optimality**



Efficiency



**Outlier
Robustness**



Generalization

Prior Methods

RANSAC-based



***Global
Optimality***



Efficiency



***Outlier
Robustness***



Generalization

Branch-and-Bound



***Global
Optimality***



Efficiency



***Outlier
Robustness***



Generalization

Learning-based



***Global
Optimality***



Efficiency



***Outlier
Robustness***



Generalization

Ours Method: GlobustVP

$$\begin{aligned} \min_{\mathbf{D}, \mathbf{Q}} \quad & \langle [\mathbf{D}\mathbf{N}; c\mathbf{1}_m^\top]^2, \mathbf{Q} \rangle \\ \text{s.t.} \quad & \mathbf{Q}^\top \mathbf{1}_4 = \mathbf{1}_m, (\mathbf{Q})^2 = \mathbf{Q}, \\ & [\mathbf{D}]_{3,*}^\top [\mathbf{D}]_{3,*} = 1, [\mathbf{D}]_{1,*}^\top [\mathbf{D}]_{2,*} = 0, \\ & [\mathbf{D}]_{2,*}^\top [\mathbf{D}]_{3,*} = 0, [\mathbf{D}]_{1,*}^\top [\mathbf{D}]_{3,*} = 0, \end{aligned}$$

1) Primal Problem
(Primal Problem)

Insight 1
Problem Reformulation

$$\begin{aligned} \min_{\mathbf{W}} \quad & \text{trace}(\mathbf{C}\mathbf{W}) \\ \text{s.t.} \quad & \mathbf{W}_{0,0} = \sum_{i=1}^4 \mathbf{W}_{0,4(j-1)+i}, \quad j = 1, \dots, m, \\ & \text{trace}(\{\mathbf{W}_{0,0}\}_{i,j}) = \begin{cases} 1, & i=j \\ 0, & i \neq j \end{cases} \quad \forall i, j \in \{1, 2, 3\} \\ & \mathbf{W} \succeq \mathbf{0}, \end{aligned}$$

2) SDP Problem
(Full SDP Problem)

$$\begin{aligned} \min_{\mathbf{W}} \quad & \text{trace}(\mathbf{C}\mathbf{W}) \\ \text{s.t.} \quad & \mathbf{W}_{0,0} = \sum_{i=1}^2 \mathbf{W}_{0,i,i}, \quad \forall i \in \{1, 2\}, \quad j = 1, \dots, m, \\ & \text{trace}(\mathbf{W}_{0,0,1}) = 1, \quad \mathbf{W}_{0,0,1} = \mathbf{W}_{0,0,2}, \\ & \mathbf{W}_{*,*,i} \succeq \mathbf{0}, \quad \forall i \in \{1, 2\}. \end{aligned}$$

3) Iterative SDP Problem
(Single Block SDP Problem)

Insight 2
Convex Relaxation

Insight 3
Iterative Acceleration



Global Optimality



Efficiency



Outlier Robustness



Generalizable

Insight 1: Primal Problem Reformulation

$\min_{\text{VP1, VP2, VP3, Permutation}} \text{Loss}(\text{Lines}, \text{VP1}, \text{VP2}, \text{VP3}, \text{Permutation})$
 How to represent discrete labels?

-> continuous constraint

$$q = q^2 \iff q = 1 \text{ or } q = 0$$

$$q_{\text{VP1}} + q_{\text{VP2}} + q_{\text{VP3}} + q_{\text{Outlier}} = 1$$

-> scales to all lines

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

Permutation Matrix

Column Sum

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

1	1	1	1	1	1
Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

Insight 1: Primal Problem Reformulation

Primal Problem

$$\min_{\mathbf{D}, \mathbf{Q}} \quad \langle ([\mathbf{D}\mathbf{N}; c\mathbf{1}_m^\top])^2, \mathbf{Q} \rangle$$

$$\text{s.t.} \quad \mathbf{Q}^\top \mathbf{1}_4 = \mathbf{1}_m, \quad (\mathbf{Q})^2 = \mathbf{Q},$$

$$\begin{aligned} [\mathbf{D}]_{1,*} [\mathbf{D}]_{1,*}^\top &= 1, \quad [\mathbf{D}]_{2,*} [\mathbf{D}]_{2,*}^\top = 1, \\ [\mathbf{D}]_{3,*} [\mathbf{D}]_{3,*}^\top &= 1, \quad [\mathbf{D}]_{1,*} [\mathbf{D}]_{2,*}^\top = 0, \\ [\mathbf{D}]_{2,*} [\mathbf{D}]_{3,*}^\top &= 0, \quad [\mathbf{D}]_{1,*} [\mathbf{D}]_{3,*}^\top = 0, \end{aligned}$$

Manhattan Constraint

min
VP1, VP2, VP3
Permutation Matrix

VP1	0.3	2e-4	0.2	0.6	0.2	0.1
VP2	2e-4	0.2	0.3	0.2	1e-4	0.2
VP3	0.2	0.1	0.4	0.3	0.3	1e-4
Outlier	9e-4	9e-4	9e-4	9e-4	9e-4	9e-4
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

Column Sum

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

1	1	1	1	1	1
Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

Ours Method: GlobustVP

$$\begin{aligned} \min_{\mathbf{D}, \mathbf{Q}} \quad & \langle ([\mathbf{D}\mathbf{N}; c\mathbf{1}_m]^\top)^2, \mathbf{Q} \rangle \\ \text{s.t.} \quad & \mathbf{Q}^\top \mathbf{1}_4 = \mathbf{1}_m, (\mathbf{Q})^2 = \mathbf{Q}, \\ & [\mathbf{D}]_{3,*} [\mathbf{D}]_{3,*}^\top = \mathbf{1}, [\mathbf{D}]_{1,*} [\mathbf{D}]_{2,*}^\top = 0, \\ & [\mathbf{D}]_{2,*} [\mathbf{D}]_{3,*}^\top = 0, [\mathbf{D}]_{1,*} [\mathbf{D}]_{3,*}^\top = 0, \end{aligned}$$

(Primal Problem)

1) Primal Problem

Insight 1

Problem Reformulation



Generalizable

Insight 2: QCQP -> Convex Relaxation -> SDP

$$\begin{aligned}
 \min_{\mathbf{D}, \mathbf{Q}} \quad & \langle (\mathbf{D}\mathbf{N}; c\mathbf{1}_m^\top)^2, \mathbf{Q} \rangle \\
 \text{s.t.} \quad & \mathbf{Q}^\top \mathbf{1}_4 = \mathbf{1}_m, (\mathbf{Q})^2 = \mathbf{Q}, \\
 & [\mathbf{D}]_{3,*} [\mathbf{D}]_{3,*}^\top = 1, [\mathbf{D}]_{1,*} [\mathbf{D}]_{2,*}^\top = 0, \\
 & [\mathbf{D}]_{2,*} [\mathbf{D}]_{3,*}^\top = 0, [\mathbf{D}]_{1,*} [\mathbf{D}]_{3,*}^\top = 0,
 \end{aligned}$$

1) Primal Problem
(Primal Problem)

$$\begin{aligned}
 \min_{\omega} \quad & \omega^\top \mathbf{C} \omega \\
 \text{s.t.} \quad & \omega_0 \omega_0^\top = \sum_{j=1}^4 \omega_j \omega_j^\top, \quad j = 1, \dots, m, \\
 & \{\omega_0\}_1^\top \{\omega_0\}_1 = 1, \quad \{\omega_0\}_2^\top \{\omega_0\}_2 = 1, \\
 & \{\omega_0\}_3^\top \{\omega_0\}_3 = 1, \quad \{\omega_0\}_1^\top \{\omega_0\}_2 = 0, \\
 & \{\omega_0\}_1^\top \{\omega_0\}_3 = 0, \quad \{\omega_0\}_2^\top \{\omega_0\}_3 = 0.
 \end{aligned}$$

Quadratically Constrained Quadratic Program (QCQP) Problem
(Full QCQP Problem)

Equivalent to Higher Dimension QCQP

Insight 2: QCQP $\rightarrow$ Convex Relaxation $\rightarrow$ SDP

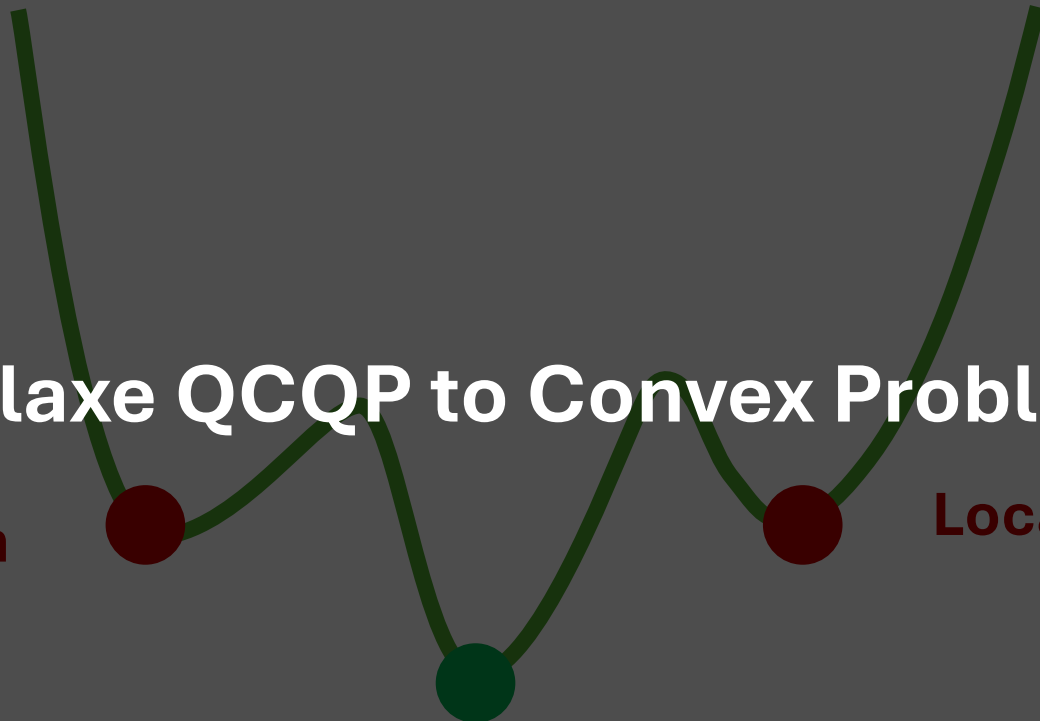
Non-convex
QCQP

Relax QCQP to Convex Problem

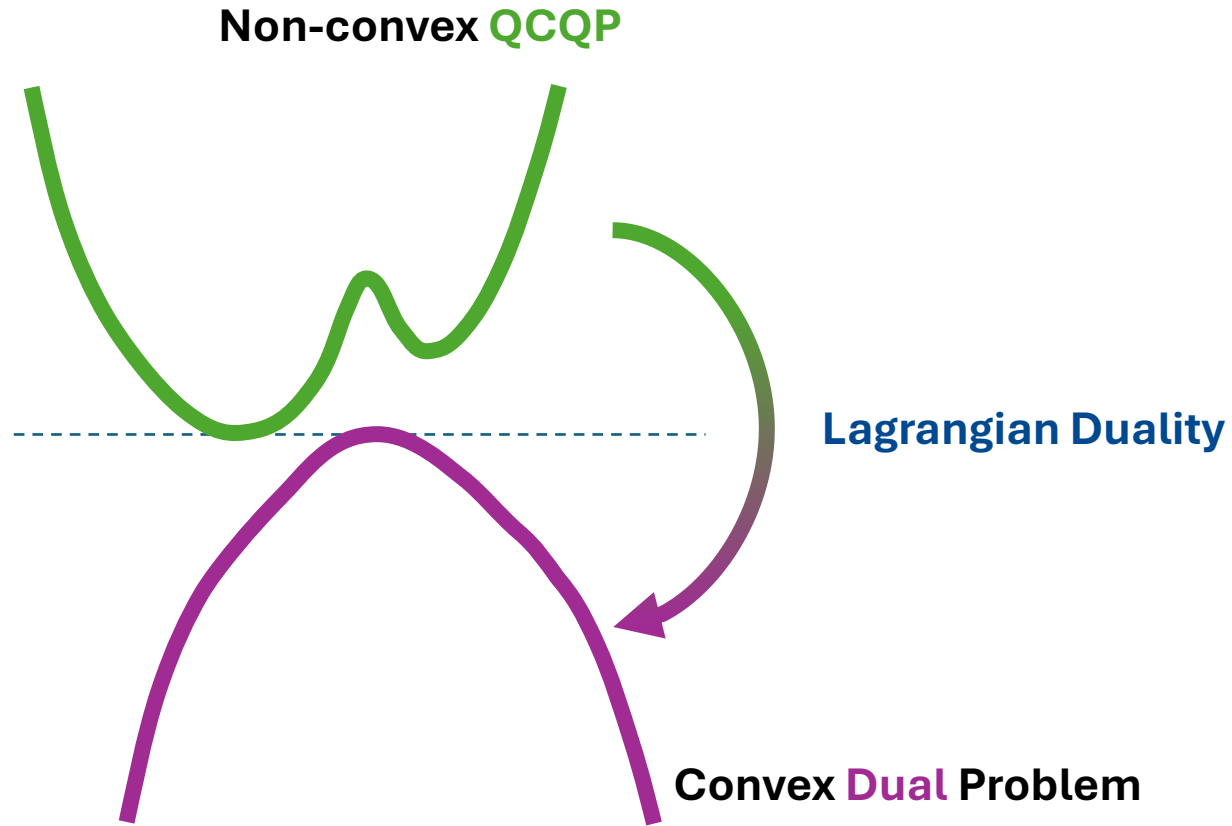
Local Minimum

Local Minimum

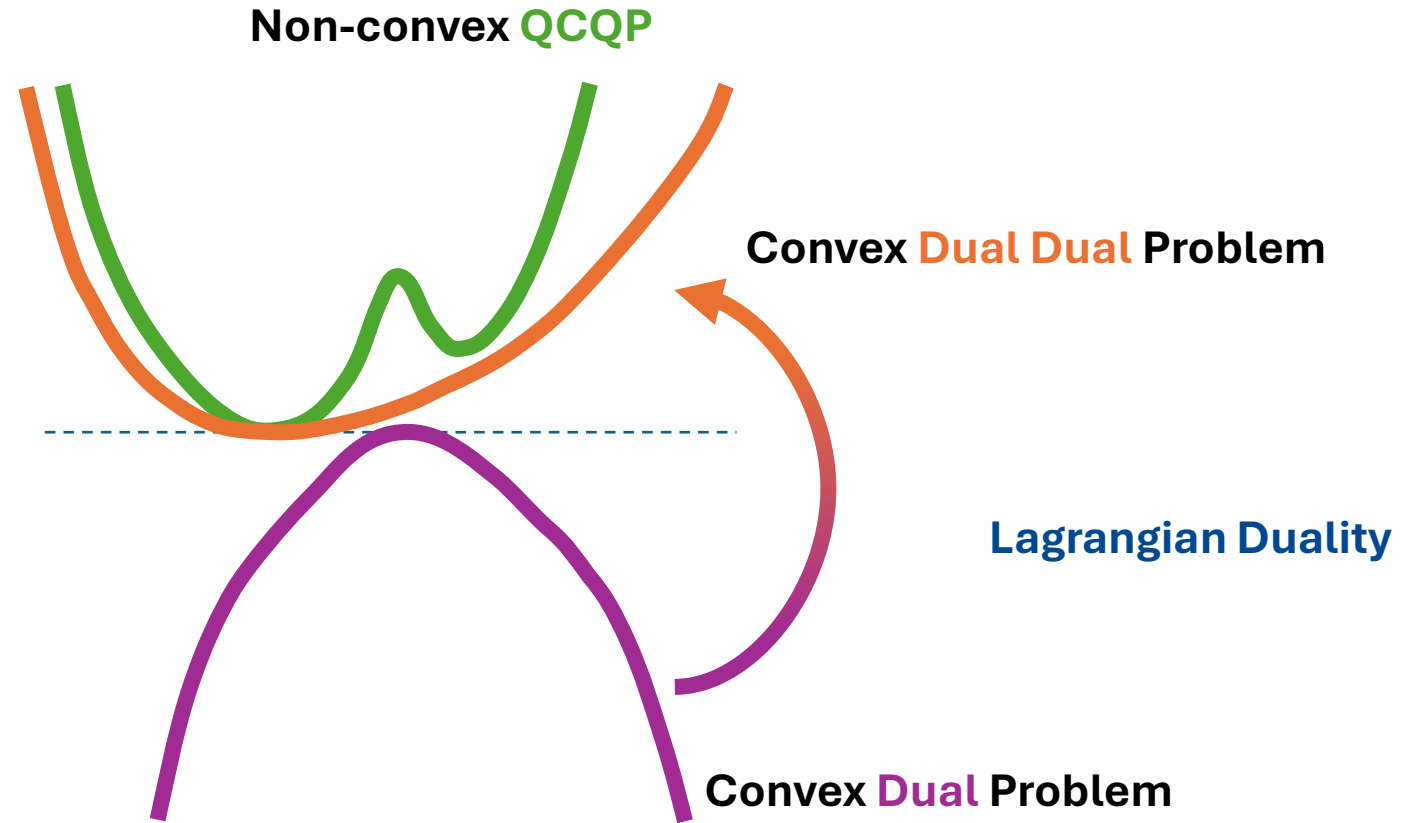
Global Minimum



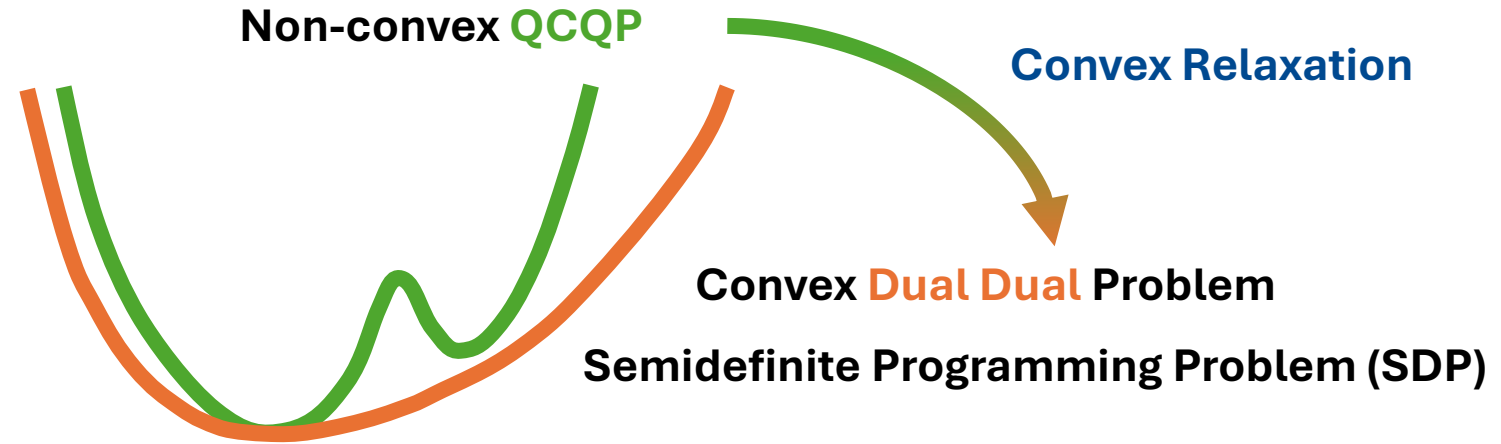
Insight 2: QCQP $\rightarrow$ Convex Relaxation $\rightarrow$ SDP



Insight 2: QCQP $\rightarrow$ Convex Relaxation $\rightarrow$ SDP



Insight 2: QCQP -> Convex Relaxation -> SDP



$$\begin{aligned}
 \min_{\omega} \quad & \omega^\top C \omega \\
 \text{s.t.} \quad & \omega_0 \omega_0^\top = \sum_{i=1}^4 \omega_0 \omega_{i,j}^\top, \quad j = 1, \dots, m, \\
 & \omega_0 \omega_{i,j}^\top = \omega_{i,j} \omega_0^\top, \quad i = 1, \dots, 4, \\
 & \{\omega_0\}_1^\top \{\omega_0\}_1 = 1, \quad \{\omega_0\}_2^\top \{\omega_0\}_2 = 1, \\
 & \{\omega_0\}_3^\top \{\omega_0\}_3 = 1, \quad \{\omega_0\}_1^\top \{\omega_0\}_2 = 0, \\
 & \{\omega_0\}_1^\top \{\omega_0\}_3 = 0, \quad \{\omega_0\}_2^\top \{\omega_0\}_3 = 0.
 \end{aligned}$$

QCQP Problem
(Full QCQP Problem)

equivalent under

 tight relaxation

$$\begin{aligned}
 \min_{\mathbf{W}} \quad & \text{trace}(\mathbf{C}\mathbf{W}) \\
 \text{s.t.} \quad & \mathbf{W}_{0,0} = \sum_{i=1}^4 \mathbf{W}_{0,4(j-1)+i}, \quad j = 1, \dots, m, \\
 & \mathbf{W}_{0,k} = \mathbf{W}_{k,0}^\top, \quad k = 1, \dots, 4, \\
 & \text{trace}(\{\mathbf{W}_{0,0}\}_{i,j}) = \begin{cases} 1, & i = j \\ 0, & i \neq j \end{cases} \quad \forall i, j \in \{1, 2, 3\} \\
 & \mathbf{W} \succeq 0,
 \end{aligned}$$

SDP Problem
(Full SDP Problem)

Ours Method: GlobustVP

$$\begin{aligned} \min_{\mathbf{D}, \mathbf{Q}} \quad & \langle [\mathbf{D}\mathbf{N}; c\mathbf{1}_m^\top]^2, \mathbf{Q} \rangle \\ \text{s.t.} \quad & \mathbf{Q}^\top \mathbf{1}_4 = \mathbf{1}_m, (\mathbf{Q})^2 = \mathbf{Q}, \\ & [\mathbf{D}]_{3,*} [\mathbf{D}]_{3,*}^\top = \mathbf{1}, [\mathbf{D}]_{1,*} [\mathbf{D}]_{2,*}^\top = 0, \\ & [\mathbf{D}]_{2,*} [\mathbf{D}]_{3,*}^\top = 0, [\mathbf{D}]_{1,*} [\mathbf{D}]_{3,*}^\top = 0, \end{aligned}$$

(Primal Problem)

Insight 1
Problem Reformulation

$$\begin{aligned} \min_{\mathbf{W}} \quad & \text{trace}(\mathbf{C}\mathbf{W}) \\ \text{s.t.} \quad & \mathbf{W}_{0,0} = \sum_{i=1}^4 \mathbf{W}_{0,4(j-1)+i}, \quad j = 1, \dots, m, \\ & \text{trace}(\{\mathbf{W}_{0,0}\}_{i,j}) = \begin{cases} 1, & i = j \\ 0, & i \neq j \end{cases} \quad \forall i, j \in \{1, 2, 3\} \\ & \mathbf{W} \succeq 0, \end{aligned}$$

(Full SDP Problem)

Insight 2
Convex Relaxation



**Global
Optimality**



**Outlier
Robustness**



Generalizable

Insight 3: Iterative SDP

$$\min_{\mathbf{W}} \text{trace}(\mathbf{C}\mathbf{W})$$

$$\text{s.t. } \mathbf{W}_{0,0} = \sum_{i=1}^4 \mathbf{W}_{0,4(j-1)+i}, \quad j = 1, \dots, m,$$

2) SDP Problem

$$\text{trace}(\{\mathbf{W}_{0,0}\}_{i,j}) = \begin{cases} 1, & i = j \\ 0, & i \neq j \end{cases} \quad \forall i, j \in \{1, 2, 3\}$$

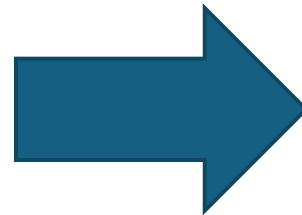
$$\mathbf{W} \succeq \mathbf{0},$$

(Full SDP Problem)

Large SDP problem is not efficient enough

VP1	0.3	2e ⁻⁴	0.2	0.6	0.2	0.1
VP2	2e ⁻⁴	0.2	0.3	0.2	1e ⁻⁴	0.2
VP3	0.2	0.1	0.4	0.3	0.3	1e ⁻⁴
Outlier	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

VP1	0	1	0	0	0	0
VP2	1	0	0	0	1	0
VP3	0	0	0	0	0	1
Outlier	0	0	1	1	0	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6



$$\min_{\mathbf{W}} \text{trace}(\mathbf{C}\mathbf{W})$$

$$\text{s.t. } \mathbf{W}_{0,0,1} = \sum_{i=1}^2 \mathbf{W}_{0,j,i}, \quad j = 1, \dots, m,$$

3) Iterative SDP Problem

$$\text{trace}(\mathbf{W}_{0,0,1}) = 1, \quad \mathbf{W}_{0,0,1} = \mathbf{W}_{0,0,2},$$

$$\mathbf{W}_{*,*,i} \succeq \mathbf{0}, \quad \forall i \in \{1, 2\}.$$

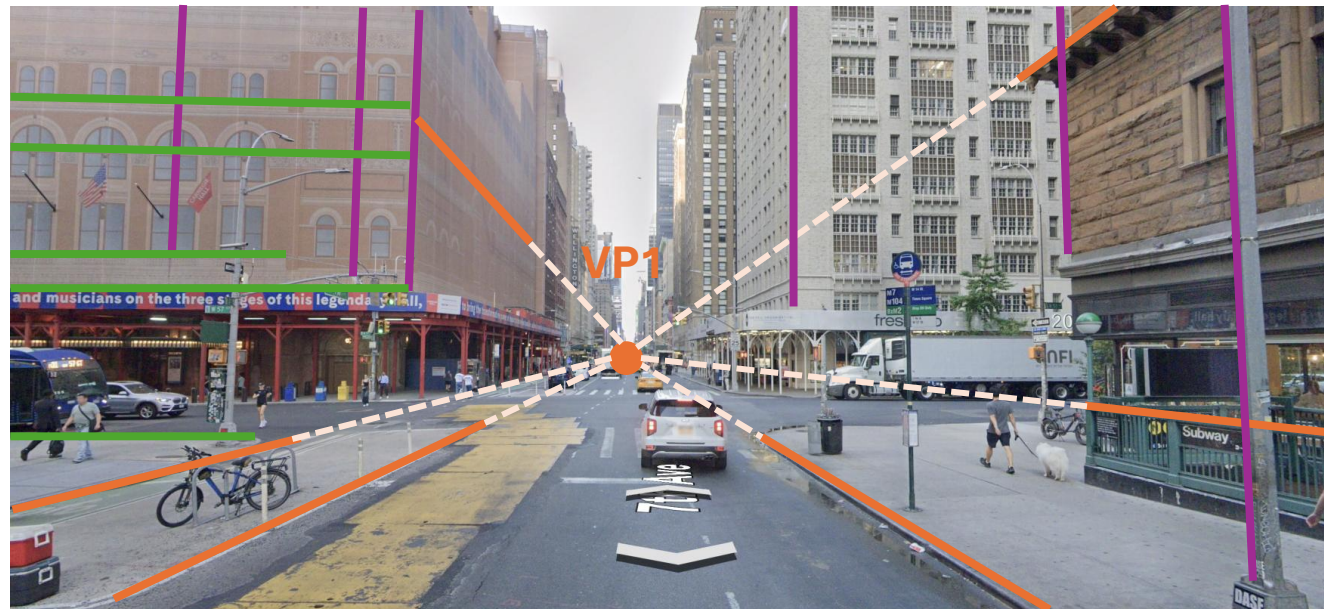
(Single Block SDP Problem)

Find VPs one by one!

VP	0.2	2e ⁻⁴	0.4	1e ⁻⁴	0.3	1e ⁻⁴
Outlier	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴	9e ⁻⁴
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

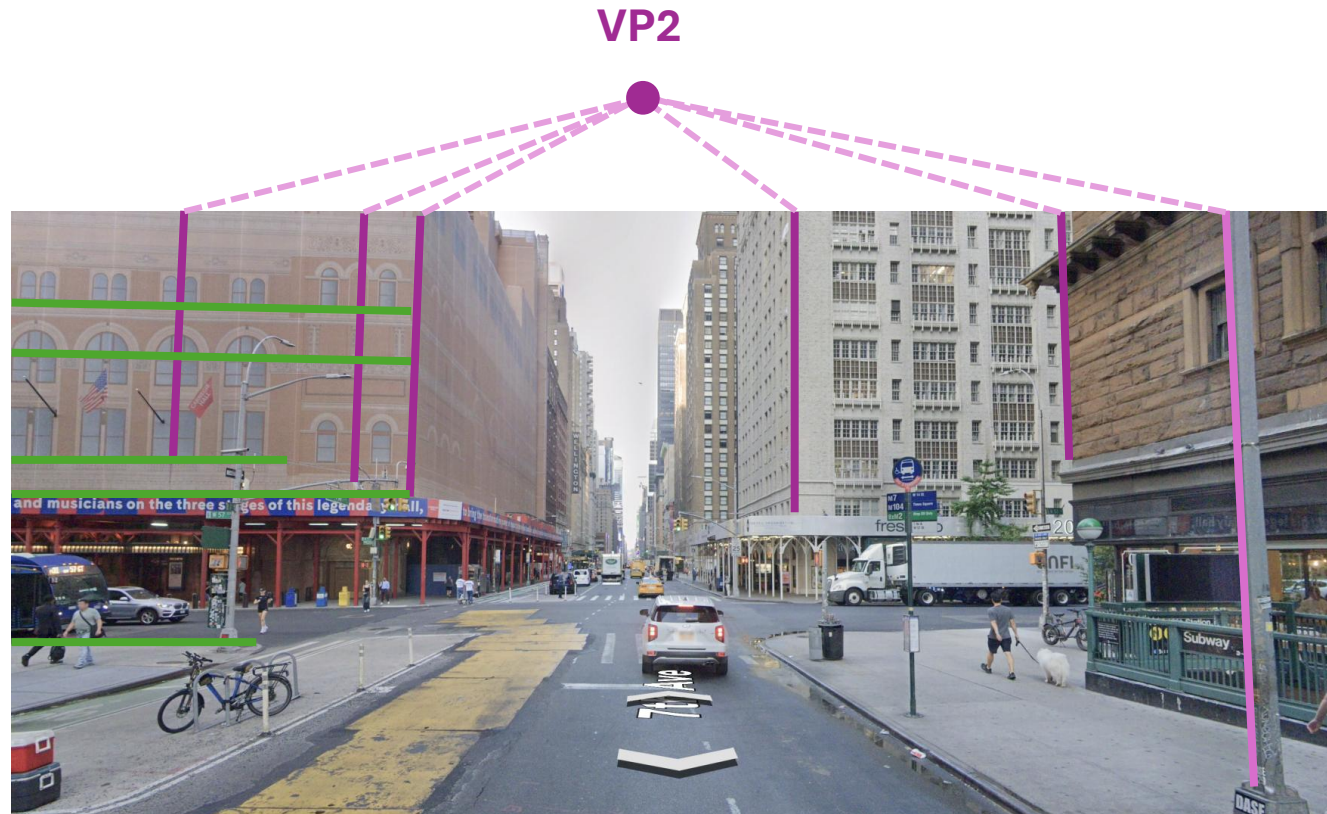
VP	0	1	0	1	0	1
Outlier	1	0	1	0	1	0
	Line 1	Line 2	Line 3	Line 4	Line 5	Line 6

Insight 3: Iterative SDP



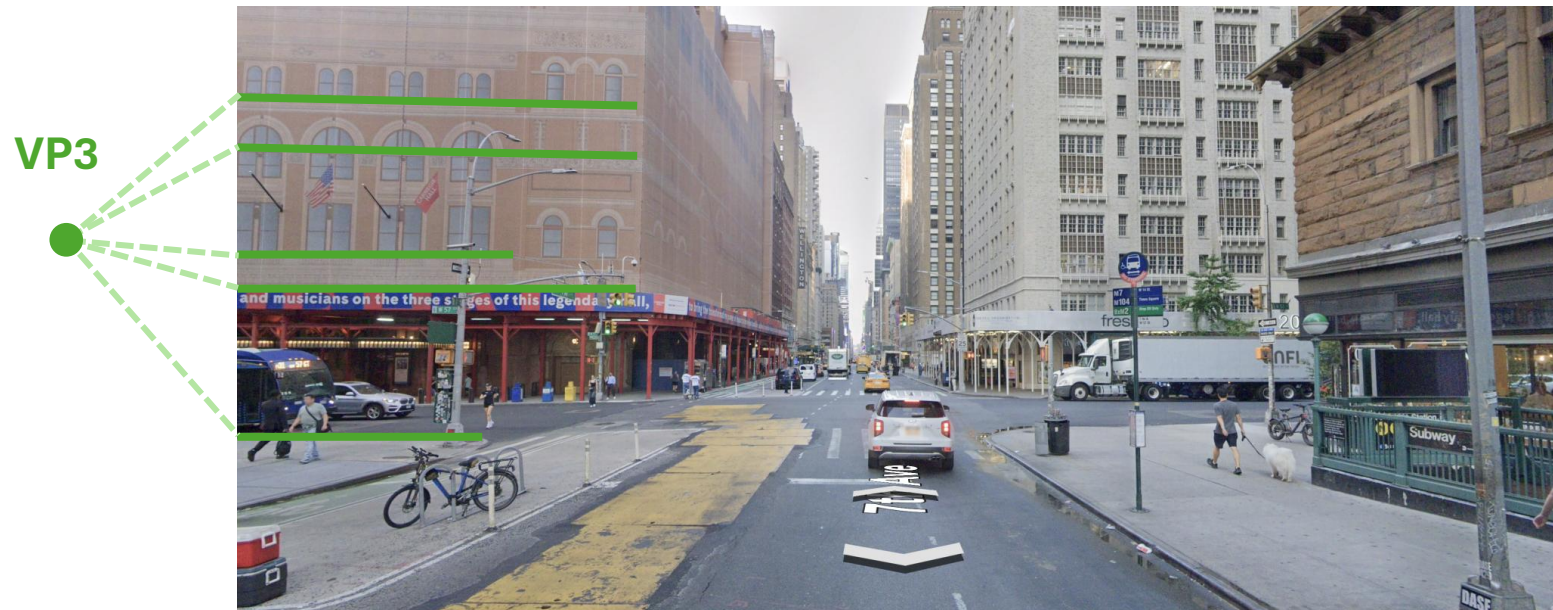
Treat **Line** and **Line** as Outliers, find **VP1**

Insight 3: Iterative SDP



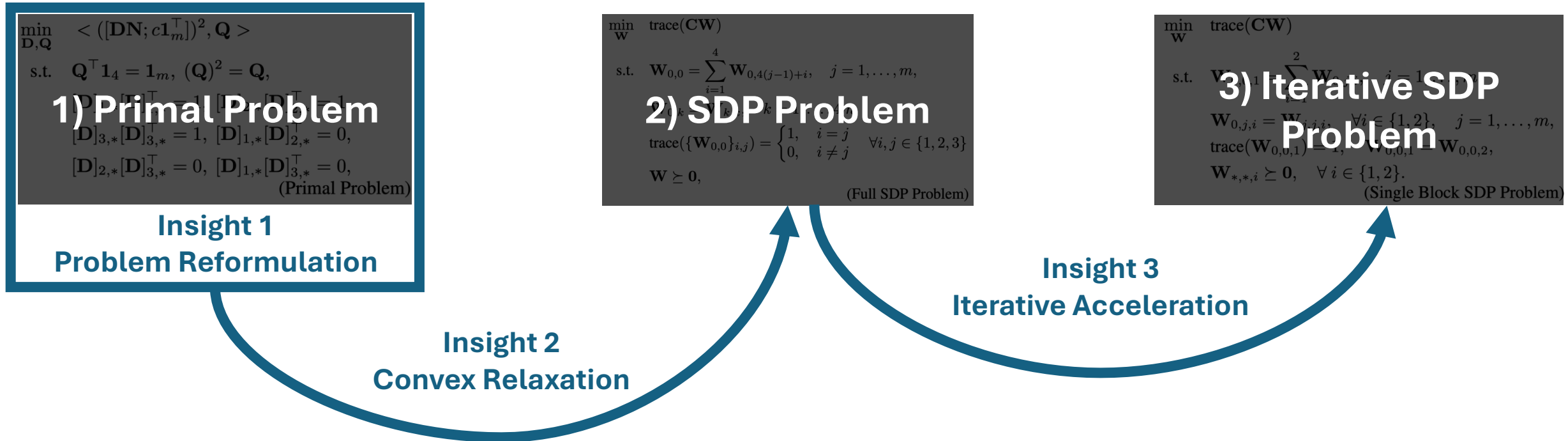
Treat **Line** as Outliers, find **VP2**

Insight 3: Iterative SDP



Find **VP3**

Ours Method: GlobustVP



**Global
Optimality**



Efficiency

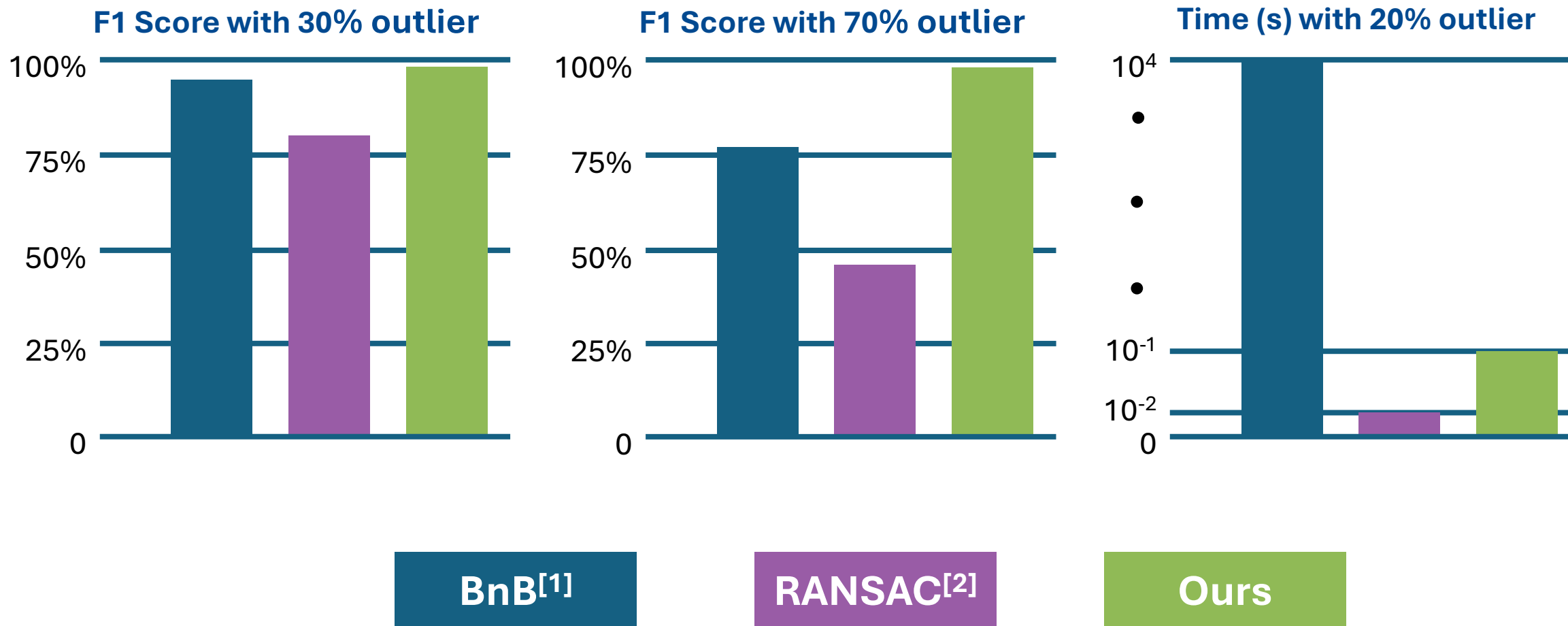


**Outlier
Robustness**



Generalizable

Synthetic Comparison



[1] Bazin J C, Seo Y, Demonceaux C, et al. Globally optimal line clustering and vanishing point estimation in manhattan world. CVPR 2012.

[2] Zhang L, Lu H, Hu X, et al. Vanishing point estimation and line classification in a manhattan world with a unifying camera model. IJCV 2016.

Real-World Comparison

F1-score↑

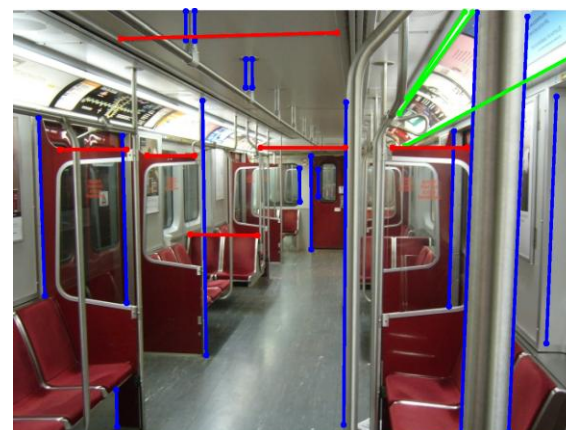
Consistency error↓



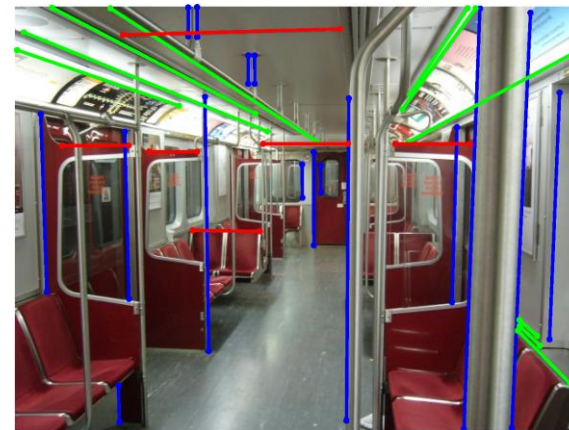
Ground Truth



BnB^[1]



RANSAC^[2]



Ours

64.29%, 2.19 pix.

85.71%, 1.01 pix.

100%, 0.41 pix.



F1-score↑

Consistency error↓

87.60%, 0.52 pix.

90.08%, 0.45 pix.

100%, 0.01 pix.

[1] Bazin J C, Seo Y, Demoncaux C, et al. Globally optimal line clustering and vanishing point estimation in manhattan world. CVPR 2012.

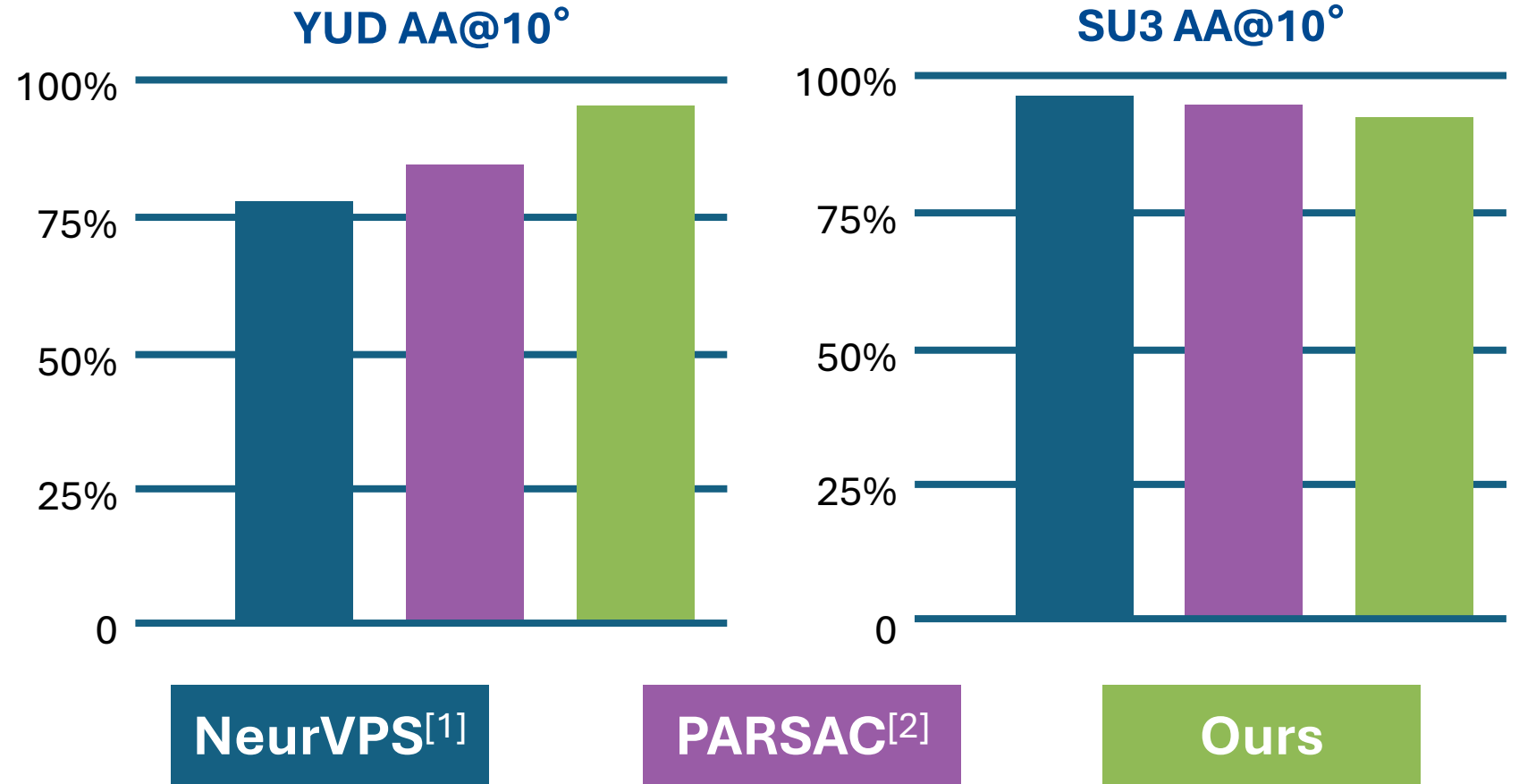
[2] Zhang L, Lu H, Hu X, et al. Vanishing point estimation and line classification in a manhattan world with a unifying camera model. IJCV 2016.

Comparison against Learning-based Method

YUD Dataset



SU3 Dataset

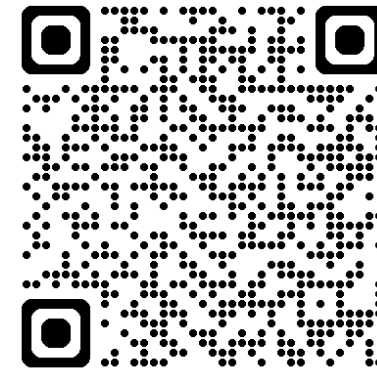
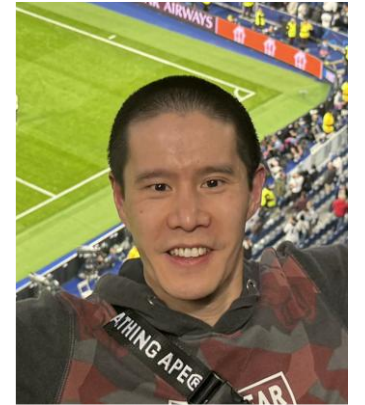
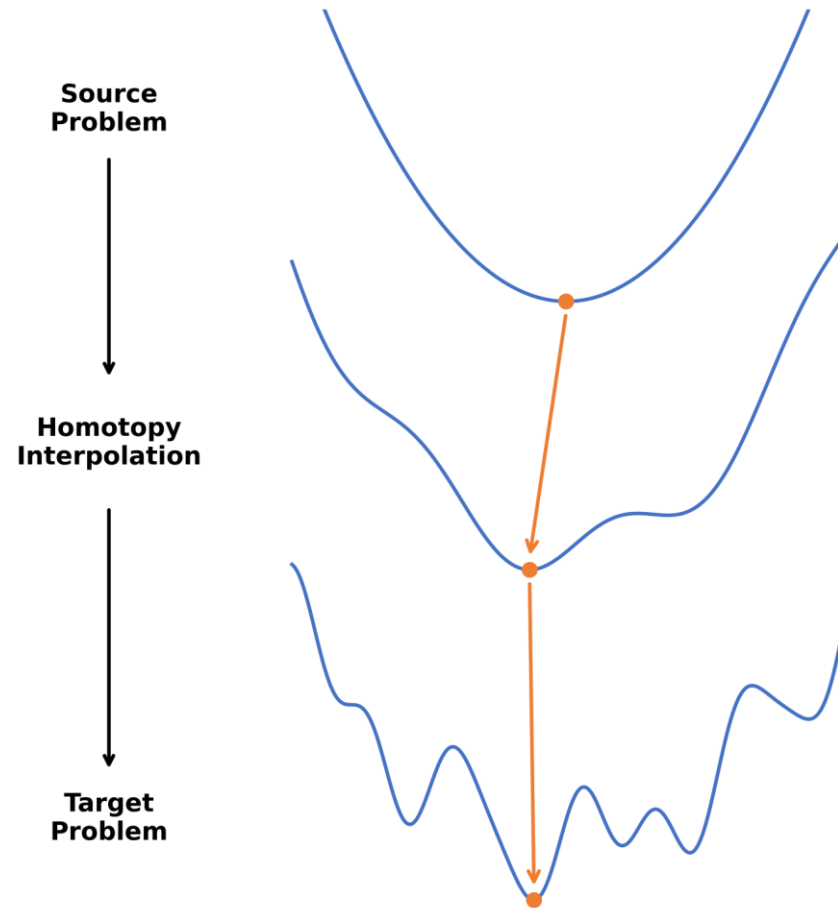


[1] Zhou Y, Qi H, Huang J, et al. Neurvps: Neural vanishing point scanning via conic convolution. NeurIPS 2019.

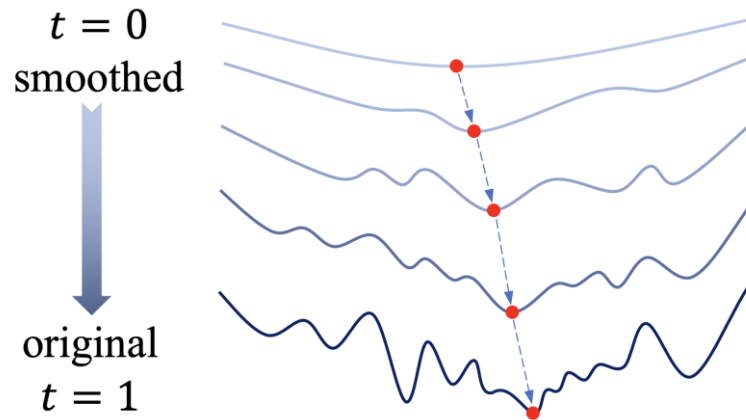
[2] Kluger F, Rosenhahn B. PARSAC: Accelerating robust multi-model fitting with parallel sample consensus. AAAI 2024.

NPC:

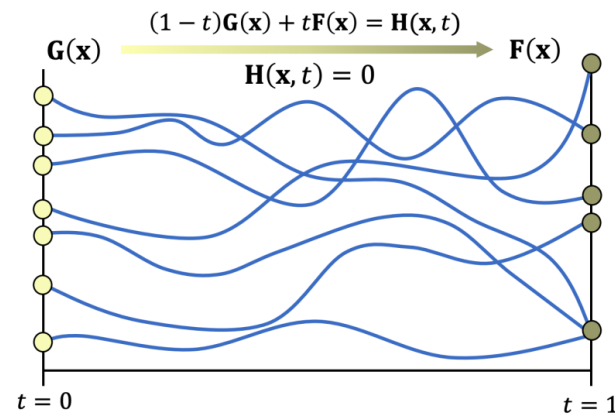
Neural Predictor-Corrector: Solving Homotopy Problems with Reinforcement Learning



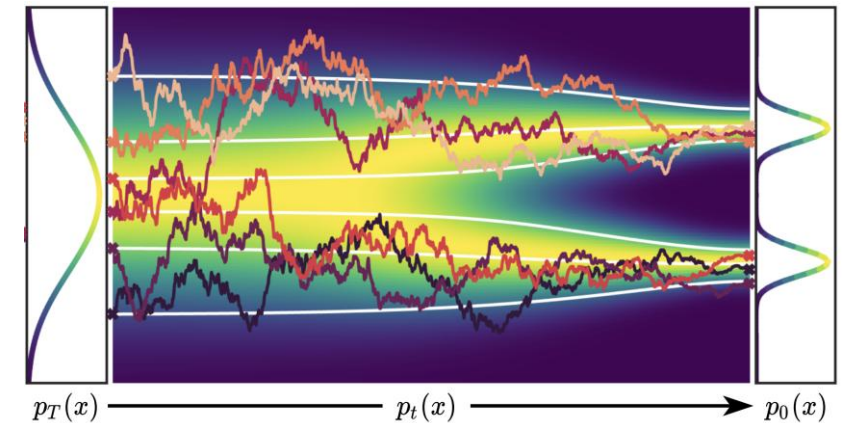
Background: Homotopy Paradigm



Optimization^[1]



Polynomial Root Finding^[2]



Sampling^[3]

A general principle for solving challenging problems

[1] Lin X, Yang Z, Zhang X, et al. Continuation path learning for homotopy optimization[C]//International Conference on Machine Learning. PMLR, 2023: 21288-21311.

[2] Zhang, Xinyue, et al. "Simulator HC: Regression-based Online Simulation of Starting Problem-Solution Pairs for Homotopy Continuation in Geometric Vision." 2025 IEEE/CVF Conference on Computer Vision and Pattern Recognition (CVPR). IEEE, 2025.

[3] Song Y, Sohl-Dickstein J, Kingma D P, et al. Score-based generative modeling through stochastic differential equations[J]. arXiv preprint arXiv:2011.13456, 2020.

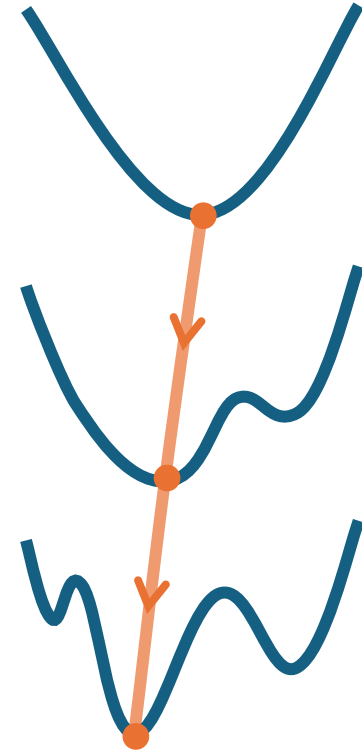
Background: Homotopy Paradigm



Easy Problem
Known Solutions



Hard Problem
Unknown Solutions



Explicit Homotopy
Interpolation Construction

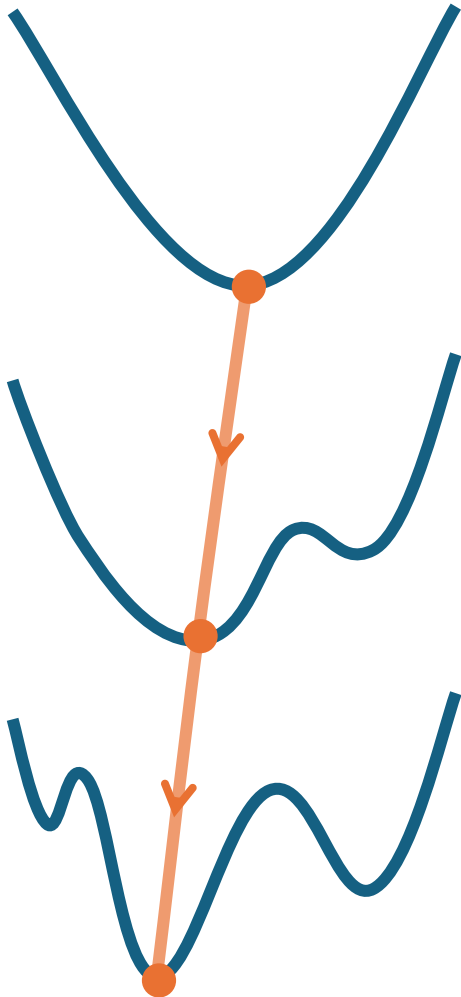


Implicit Solution
Trajectory Tracing

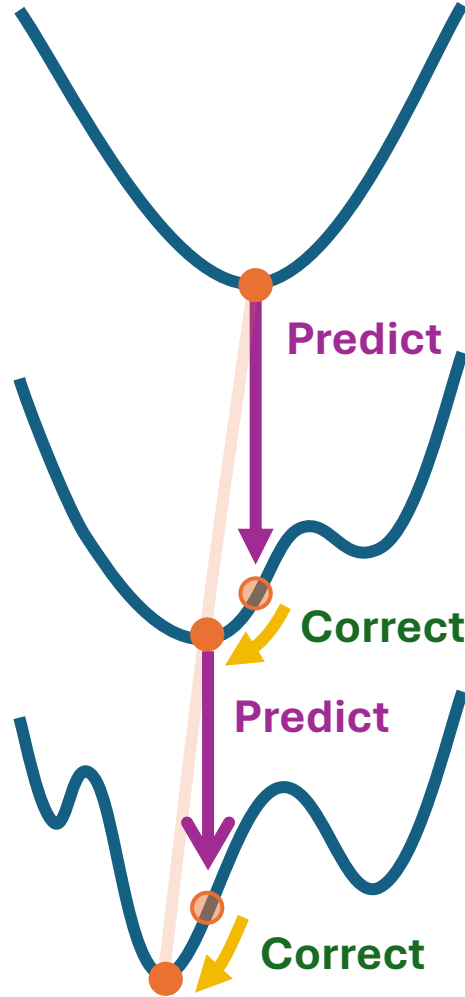
Our Scope

Motivation: Classical Predictor-Corrector

Implicit Solution Trajectory



Classical Predictor-Corrector



Algorithm

```
while  $t_n < T$  do
  Predictor: Predict next level  $t_n$ 
  Predictor: Predict  $\mathbf{x}_{t_n}$ 
  while  $H(\mathbf{x}_{t_n}, t_n) \leq \epsilon$  do
    Corrector: Correct  $\mathbf{x}_{t_n}$ 
  end
end
```

Classical PC relies on
hand-crafted heuristics

Our Method: Neural Predictor-Corrector (NPC)

Classical Predictor-Corrector

$\Delta t, \epsilon$

Algorithm 1

```
while  $t_n < T$  do
    Predictor: Predict next level  $t_n = t_{n-1} + \Delta t$ 
    Predictor: Predict  $\mathbf{x}_{t_n}$ 
    while  $H(\mathbf{x}_{t_n}, t_n) \leq \epsilon$  do
        Corrector: Correct  $\mathbf{x}_{t_n}$ 
    end
end
```

Neural Predictor-Corrector

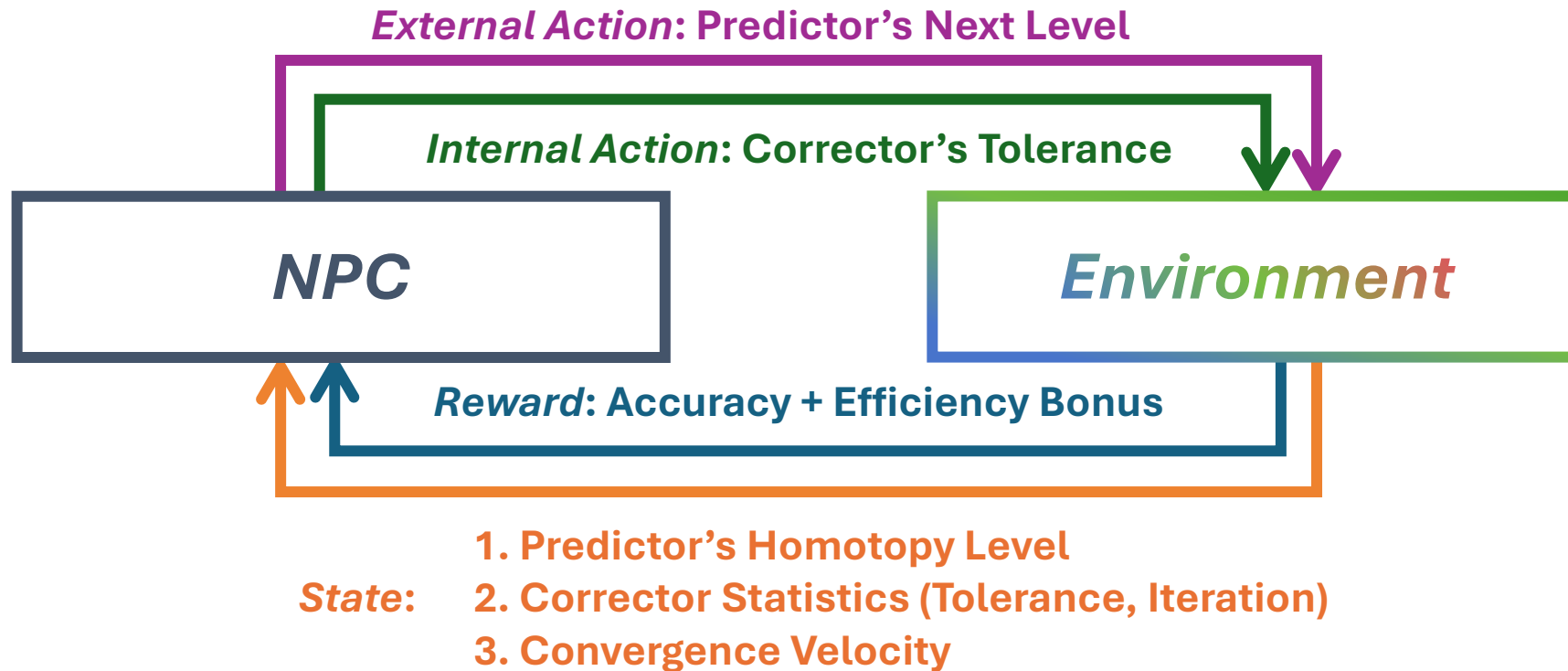
$\Delta t_n, \epsilon_n$

Algorithm 2

```
while  $t_n < T$  do
    NPC:  $\{\Delta t_n, \epsilon_n\} = \text{NN}(t_{n-1}, \epsilon_{n-1}, \tau_{n-1})$ 
    Predictor: Predict next level  $t_n = t_{n-1} + \Delta t_n$ 
    Predictor: Predict  $\mathbf{x}_{t_n}$ 
    while  $H(\mathbf{x}_{t_n}, t_n) \leq \epsilon_n$  do
        Corrector: Correct  $\mathbf{x}_{t_n}$ 
    end
    Collect corrector statistics  $\epsilon_n$ 
    Collect convergence velocity  $\tau_n$ 
end
```

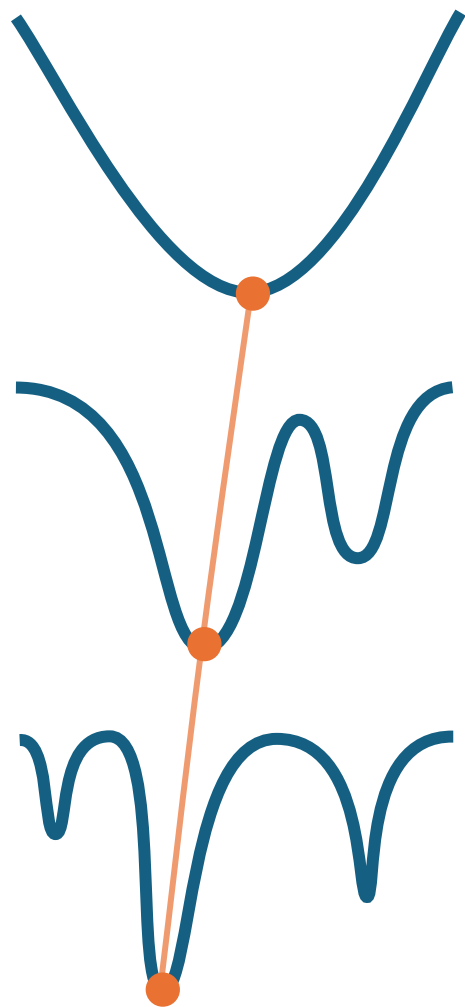
NPC replaces manual heuristics with a neural network

Our Method: Neural Predictor-Corrector (NPC)

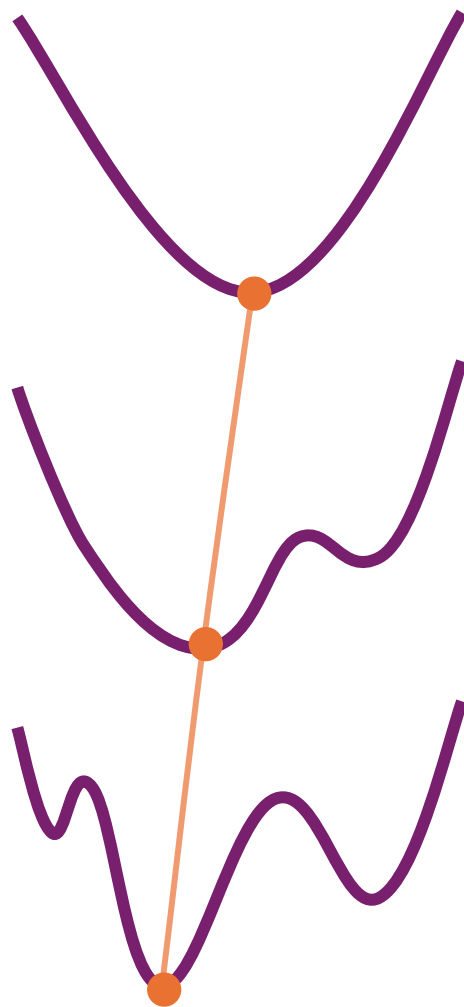


Training NPC via RL to discover optimal policies

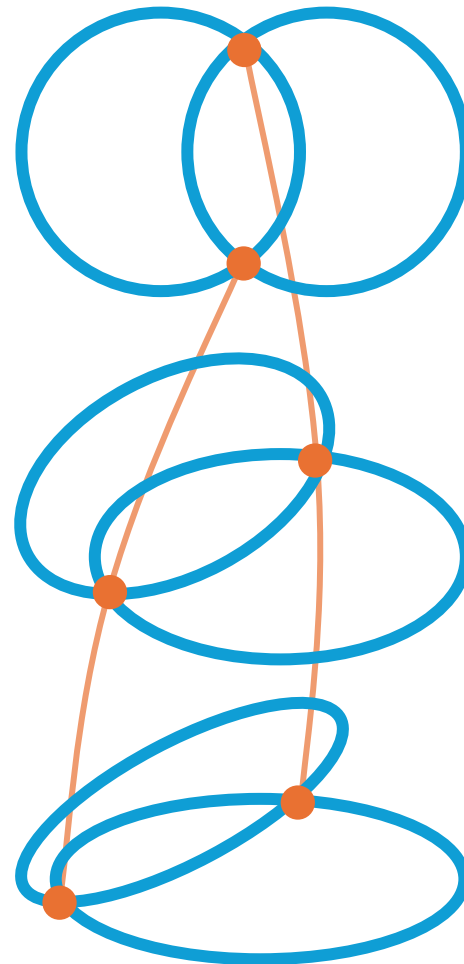
Experiments



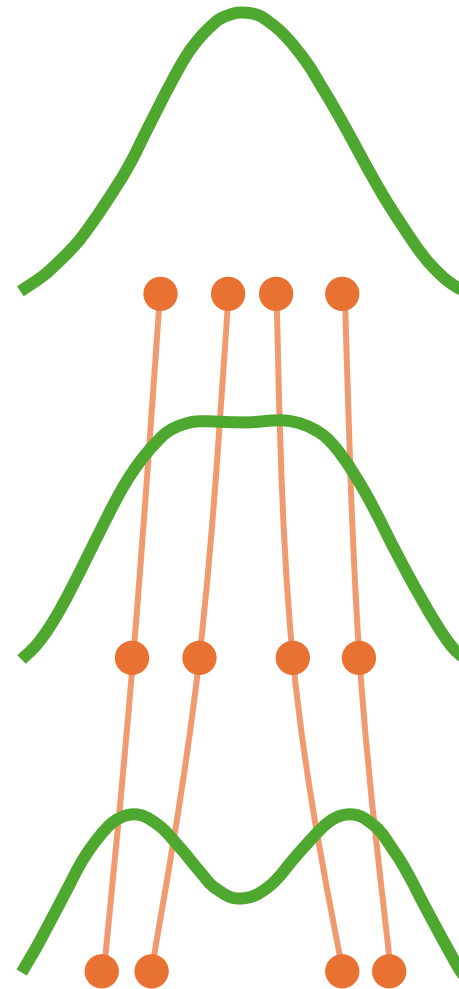
**Robust
Optimization**



**Global
Optimization**

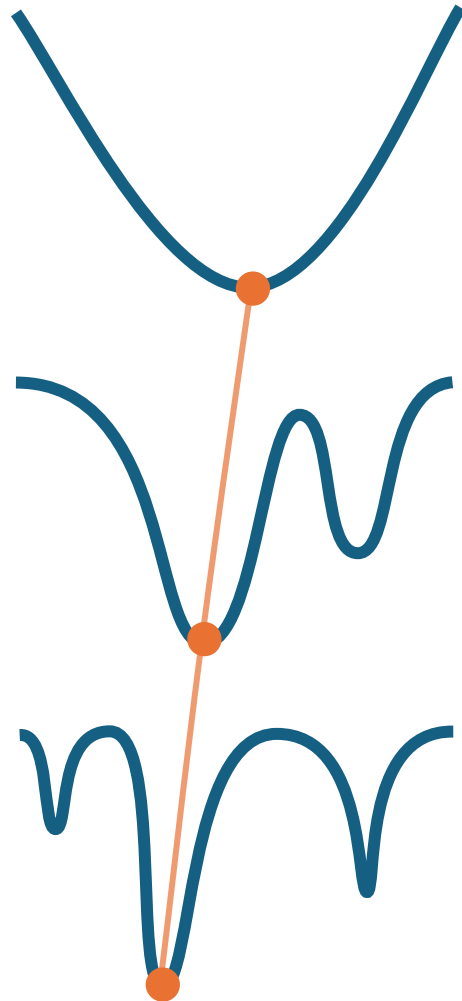


**Polynomial
Root Finding**



**Probabilistic
Sampling**

Problem 1 : Robust Optimization via GNC

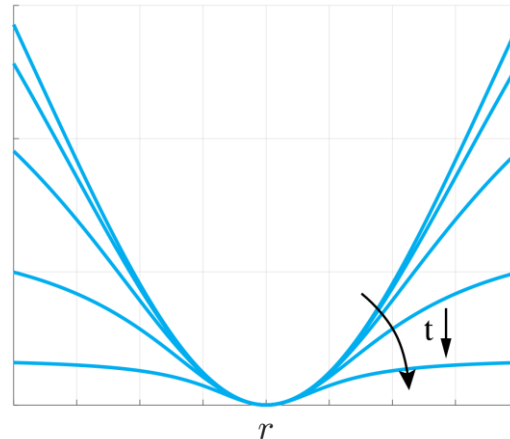


**Robust
Optimization**

Graduated Non-Convexity (GNC)^[1]

**Outer Interpolation
(Geman-McClure)**

$$H(\mathbf{x}, t) = \sum_i \frac{\bar{c}^2 r(\mathbf{x}, y_i)^2}{\bar{c}^2 + tr(\mathbf{x}, y_i)^2}$$



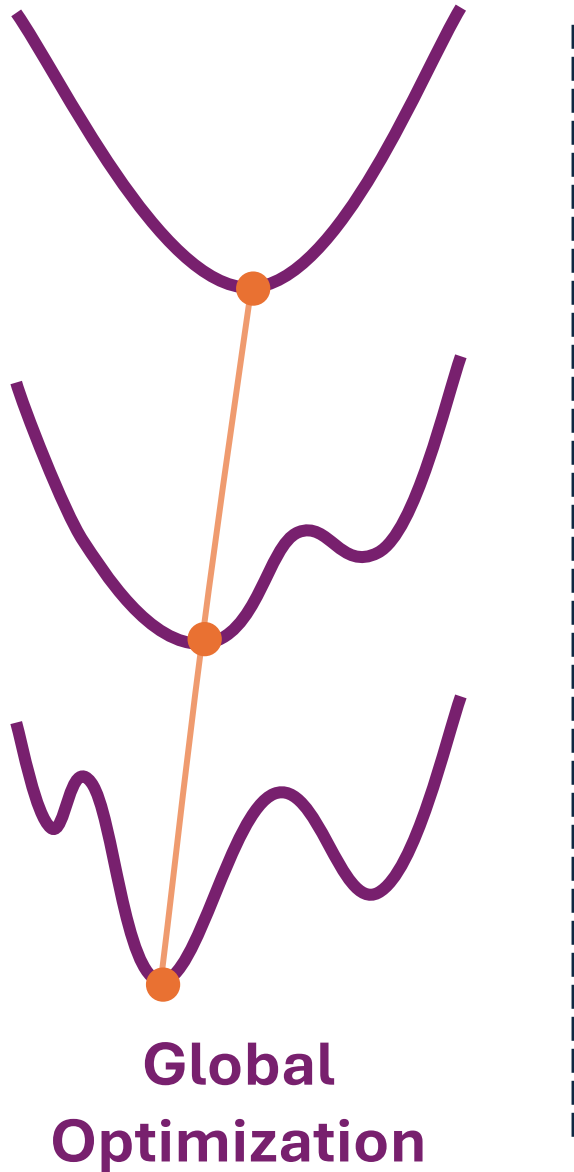
Predictor

$$\begin{aligned} t_{i+1} &= t_i + \Delta t \\ \mathbf{x}_{t_{i+1}} &= \mathbf{x}_{t_i}^* \end{aligned}$$

Corrector (*Gauss-Newton*)

$$\mathbf{x}_t^* = \arg \min_{\mathbf{x}} H(\mathbf{x}, t)$$

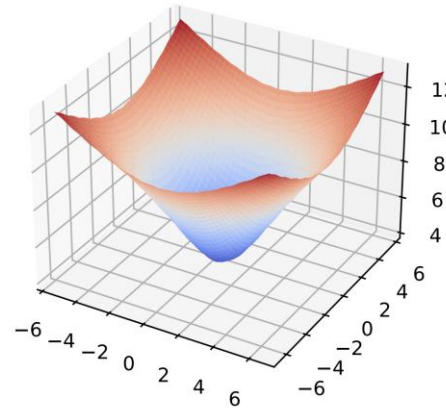
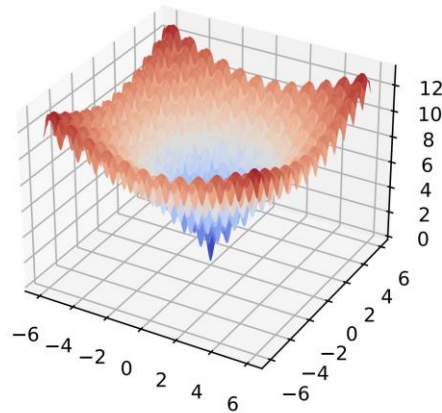
Problem 2 : Global Optimization via GH



Gaussian Homotopy (GH)^[1]

Outer Interpolation

$$H(\mathbf{x}, t) = g(\mathbf{x}) * \mathcal{N}(0, t\sigma^2)$$



Predictor

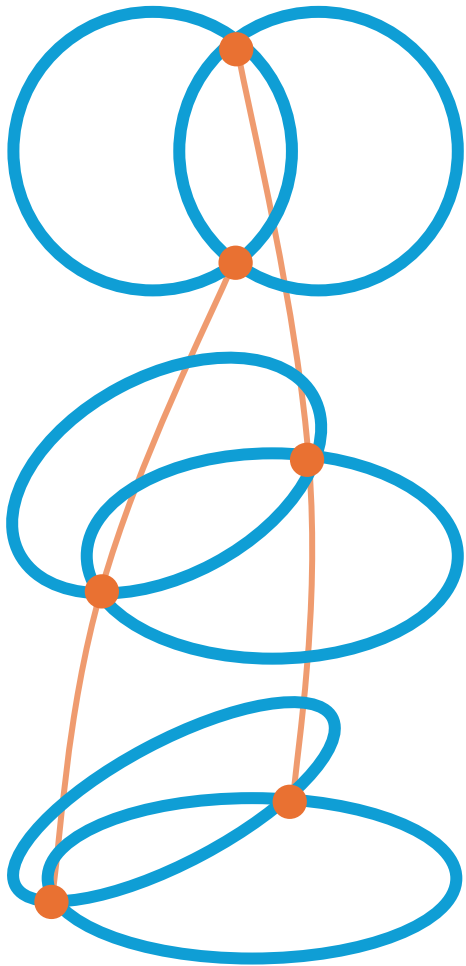
$$t_{i+1} = t_i + \Delta t$$
$$\mathbf{x}_{t_{i+1}}^* = \mathbf{x}_{t_i}^*$$

Corrector

$$\mathbf{x}_t^* = \arg \min_{\mathbf{x}} H(\mathbf{x}, t)$$

[1] Mobahi H, Fisher III J W. On the link between gaussian homotopy continuation and convex envelopes[C]//International Workshop on Energy Minimization Methods in Computer Vision and Pattern Recognition. Cham: Springer International Publishing, 2015: 43-56.

Problem 3 : Polynomial Root-Finding via HC

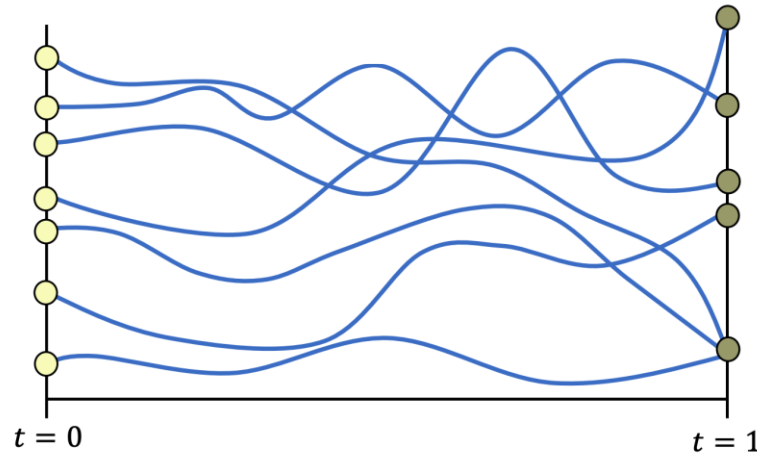


**Polynomial Root
Finding**

Homotopy Continuation (HC)^[1]

Outer Interpolation

$$H(\mathbf{x}, t) = g(\mathbf{x})(1 - t) + f(\mathbf{x})t$$



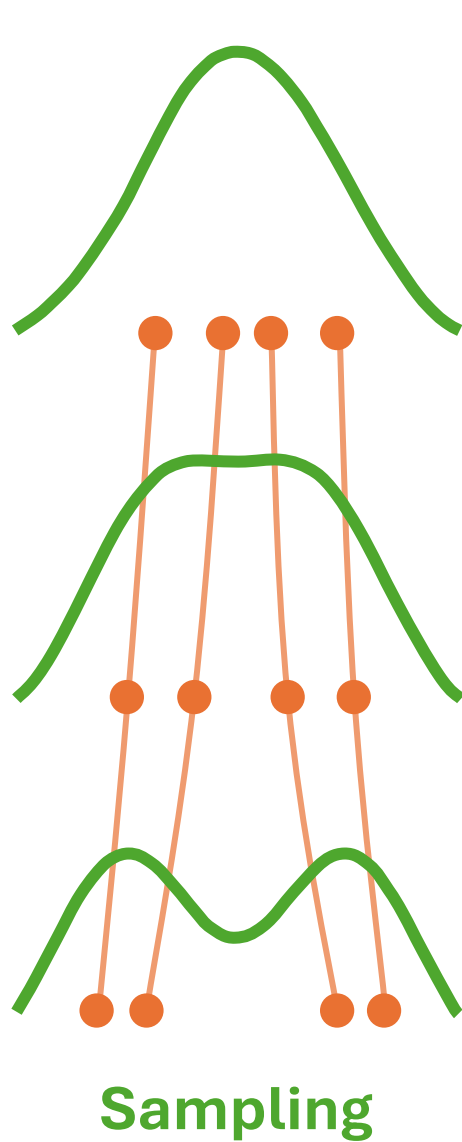
Predictor

$$t_{i+1} = t_i + \Delta t$$
$$\{\mathbf{x}_{t_{i+1}}\} = \{\mathbf{x}_{t_i}^* + \partial_t H(\mathbf{x}_{t_i}^*, t_i) \Delta t\}$$

Corrector (*Gauss-Newton*)

$$\{\mathbf{x}_t^*\} = \{H(\mathbf{x}, t) = 0\}$$

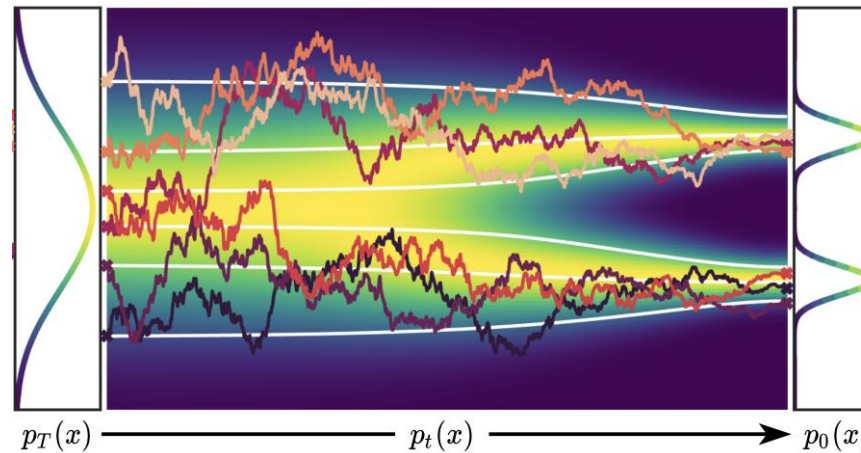
Problem 4 : Sampling via ALD



Annealed Langevin Dynamics (ALD)^[1]

Outer Interpolation

$$H(\mathbf{x}, t) \propto \exp(-g(\mathbf{x})(1 - t) - f(\mathbf{x})t)$$



Predictor

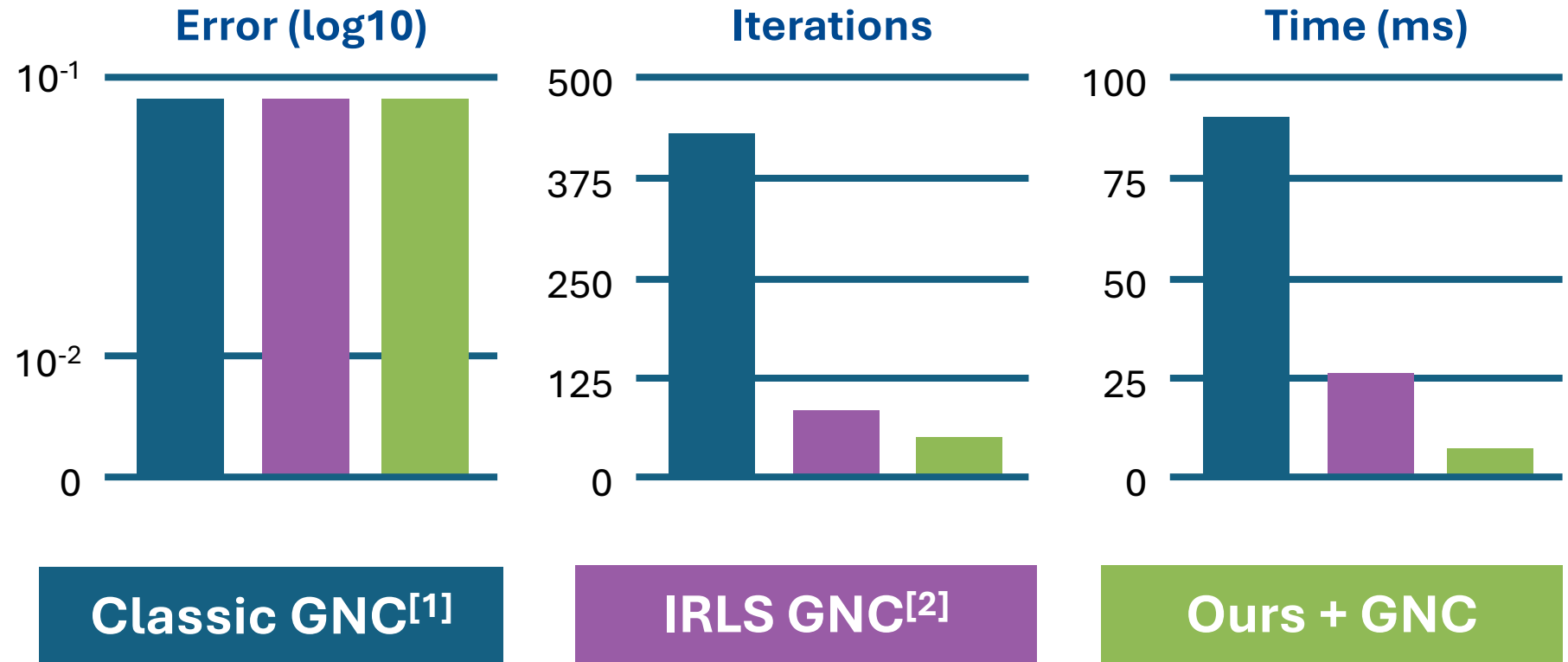
$$t_{i+1} = t_i + \Delta t$$
$$\{X_{t_{i+1}}^0\} = \{X_{t_i}^*\}$$

Corrector (LD)

$$dX_t^s = \nabla \log H(\mathbf{x}, t) ds + dW_s$$

Problem 1 : Robust Optimization via GNC

*Point Cloud
Registration
(Seq cube)*

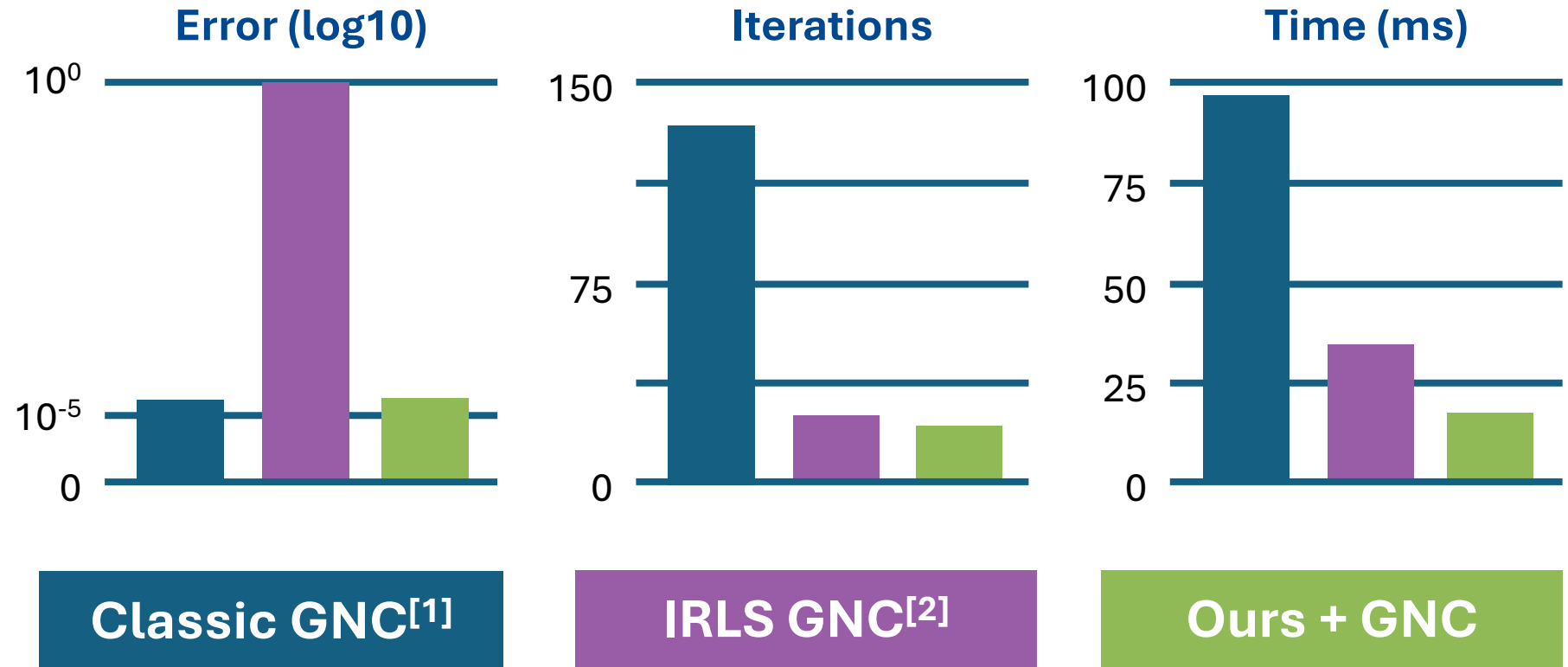


[1] Yang H, Antonante P, Tzoumas V, et al. Graduated non-convexity for robust spatial perception: From non-minimal solvers to global outlier rejection[J]. IEEE Robotics and Automation Letters, 2020, 5(2): 1127-1134.

[2] Peng L, Kümmerle C, Vidal R. On the convergence of IRLS and its variants in outlier-robust estimation[C]//Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition. 2023: 17808-17818.

Problem 1 : Robust Optimization via GNC

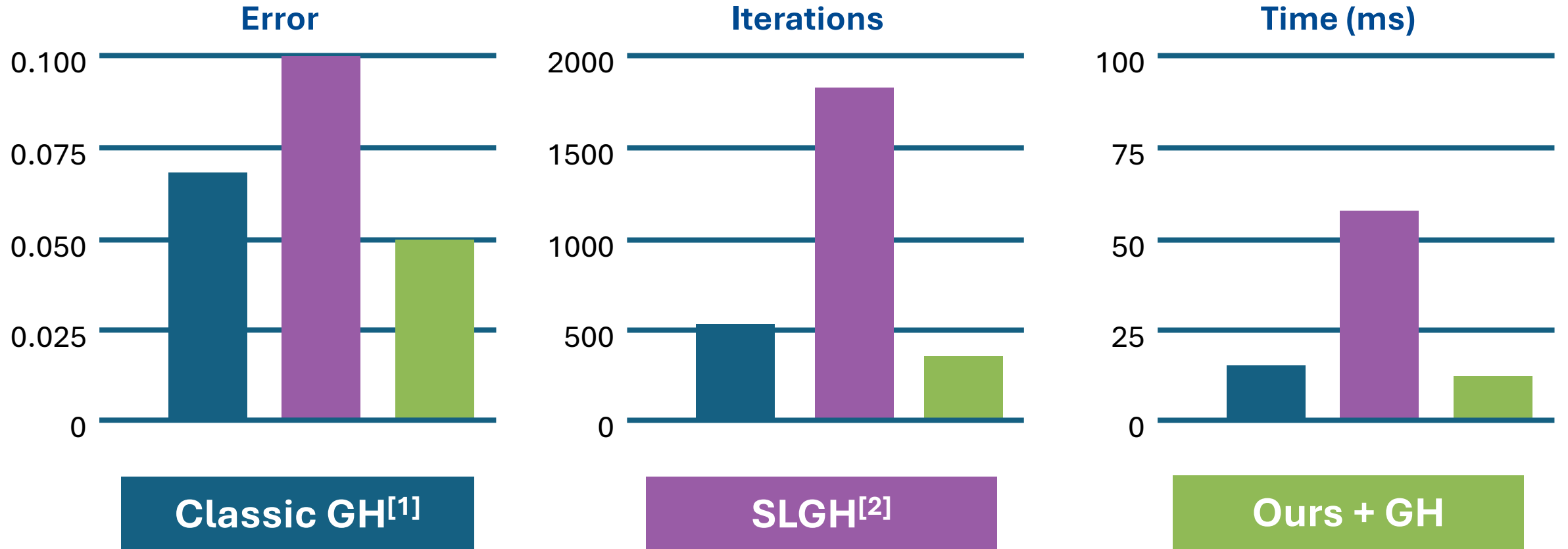
*Multi-view
Triangulation
(Seq st_pt_sq)*



[1] Yang H, Antonante P, Tzoumas V, et al. Graduated non-convexity for robust spatial perception: From non-minimal solvers to global outlier rejection[J]. IEEE Robotics and Automation Letters, 2020, 5(2): 1127-1134.

[2] Peng L, Kümmerle C, Vidal R. On the convergence of IRLS and its variants in outlier-robust estimation[C]//Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition. 2023: 17808-17818.

Problem 2 : Global Optimization via GH

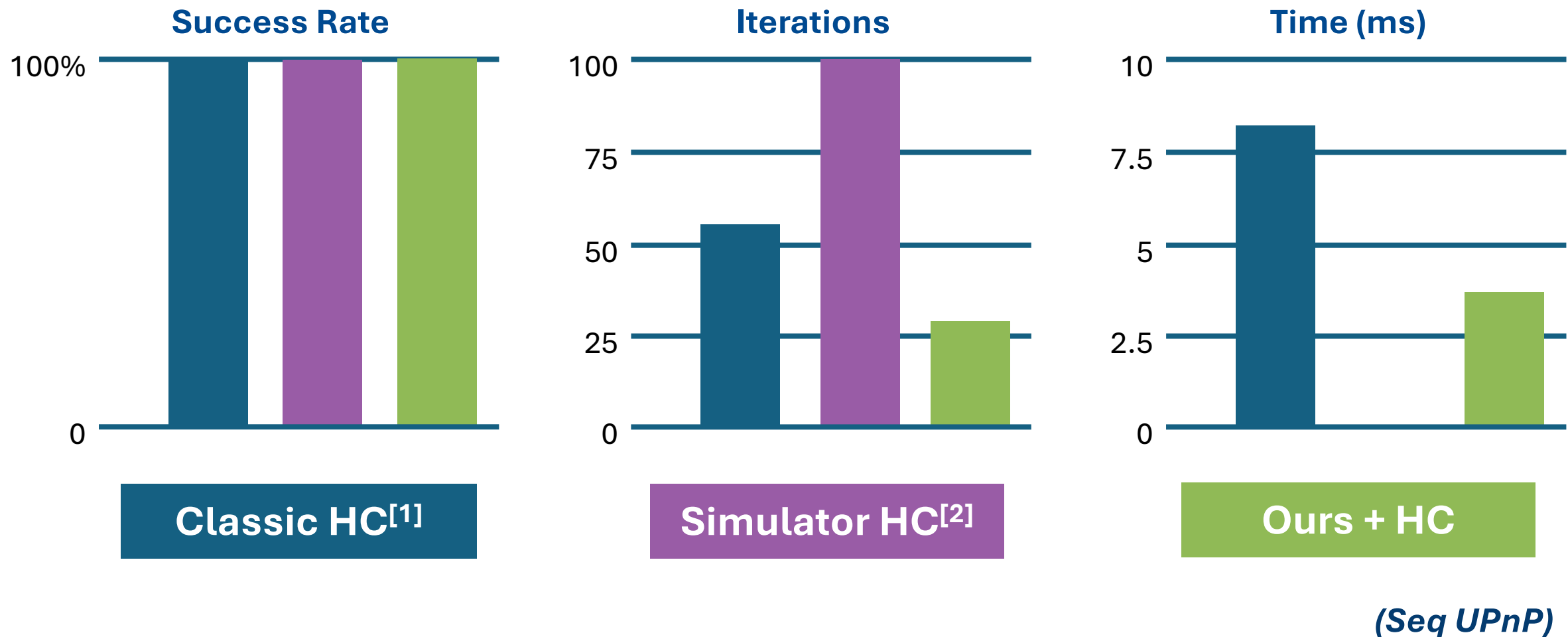


(Seq 2d_Ackley)

[1] Mobahi H, Fisher III J W. On the link between gaussian homotopy continuation and convex envelopes[C]//International Workshop on Energy Minimization Methods in Computer Vision and Pattern Recognition. Cham: Springer International Publishing, 2015: 43-56.

[2] Iwakiri H, Wang Y, Ito S, et al. Single loop gaussian homotopy method for non-convex optimization[J]. Advances in Neural Information Processing Systems, 2022,⁴⁴ 35: 7065-7076.

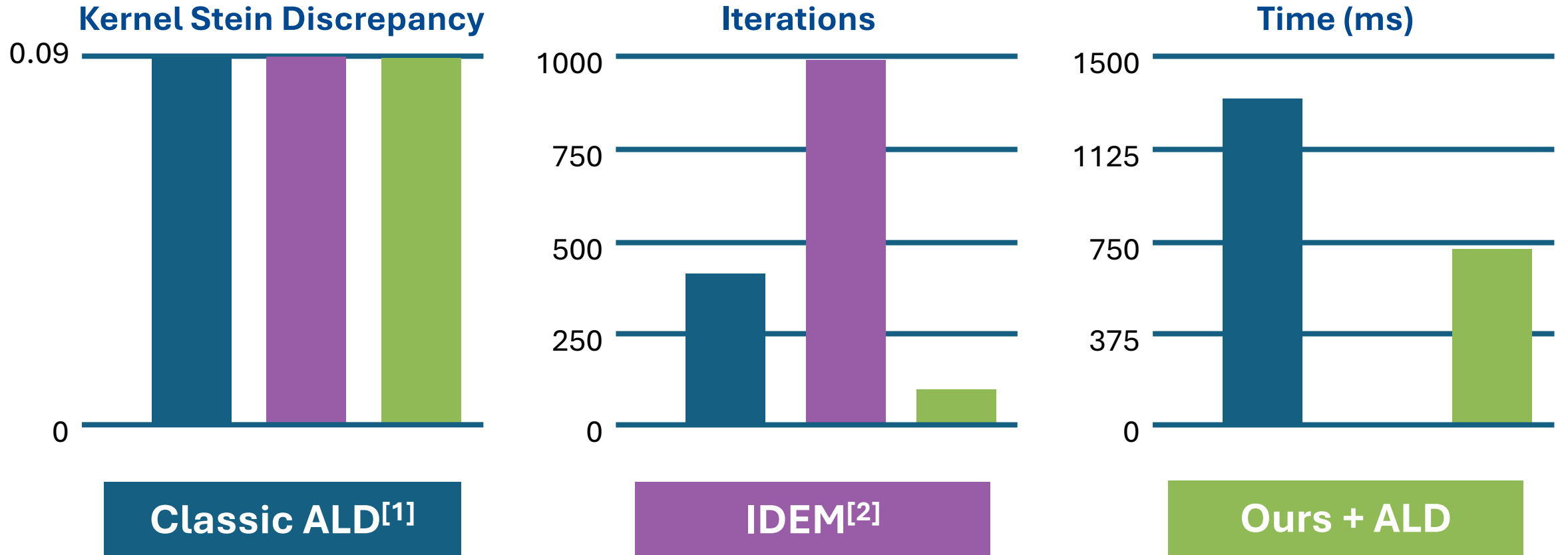
Problem 3 : Polynomial Root-Finding via HC



[1] Bates D J, Sommese A J, Hauenstein J D, et al. Numerically solving polynomial systems with Bertini[M]. Society for Industrial and Applied Mathematics, 2013.

[2] Zhang X, Dai Z, Xu W, et al. Simulator hc: Regression-based online simulation of starting problem-solution pairs for homotopy continuation in geometric vision[C]//Proceedings of the Computer Vision and Pattern Recognition Conference. 2025: 27103-27112.

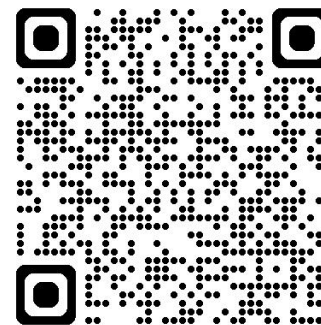
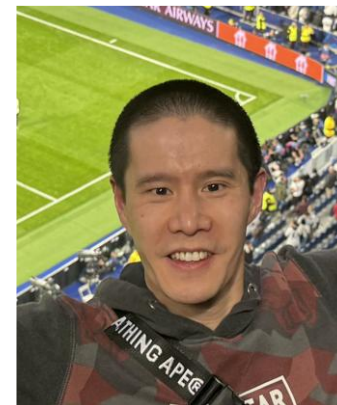
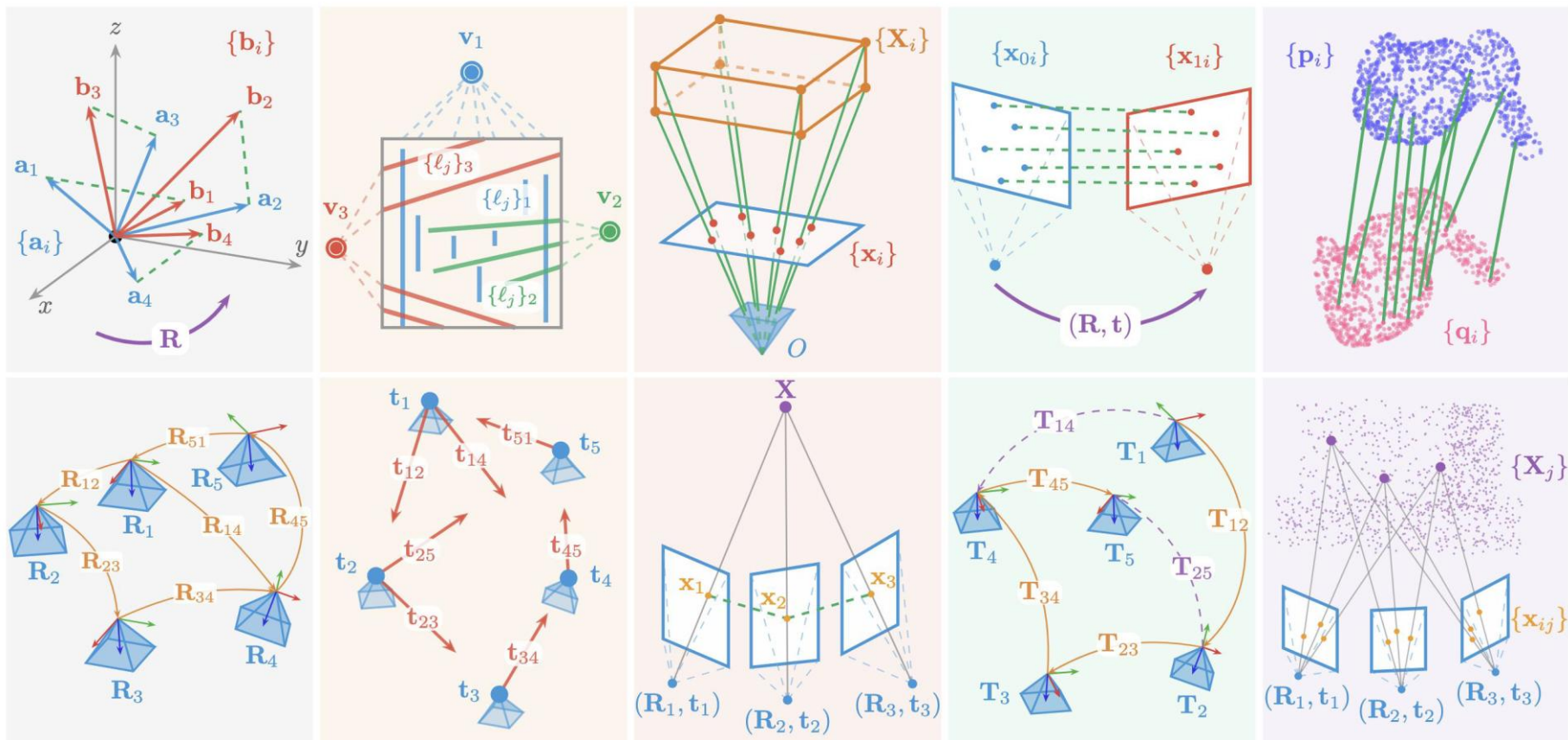
Problem 4 : Sampling via ALD



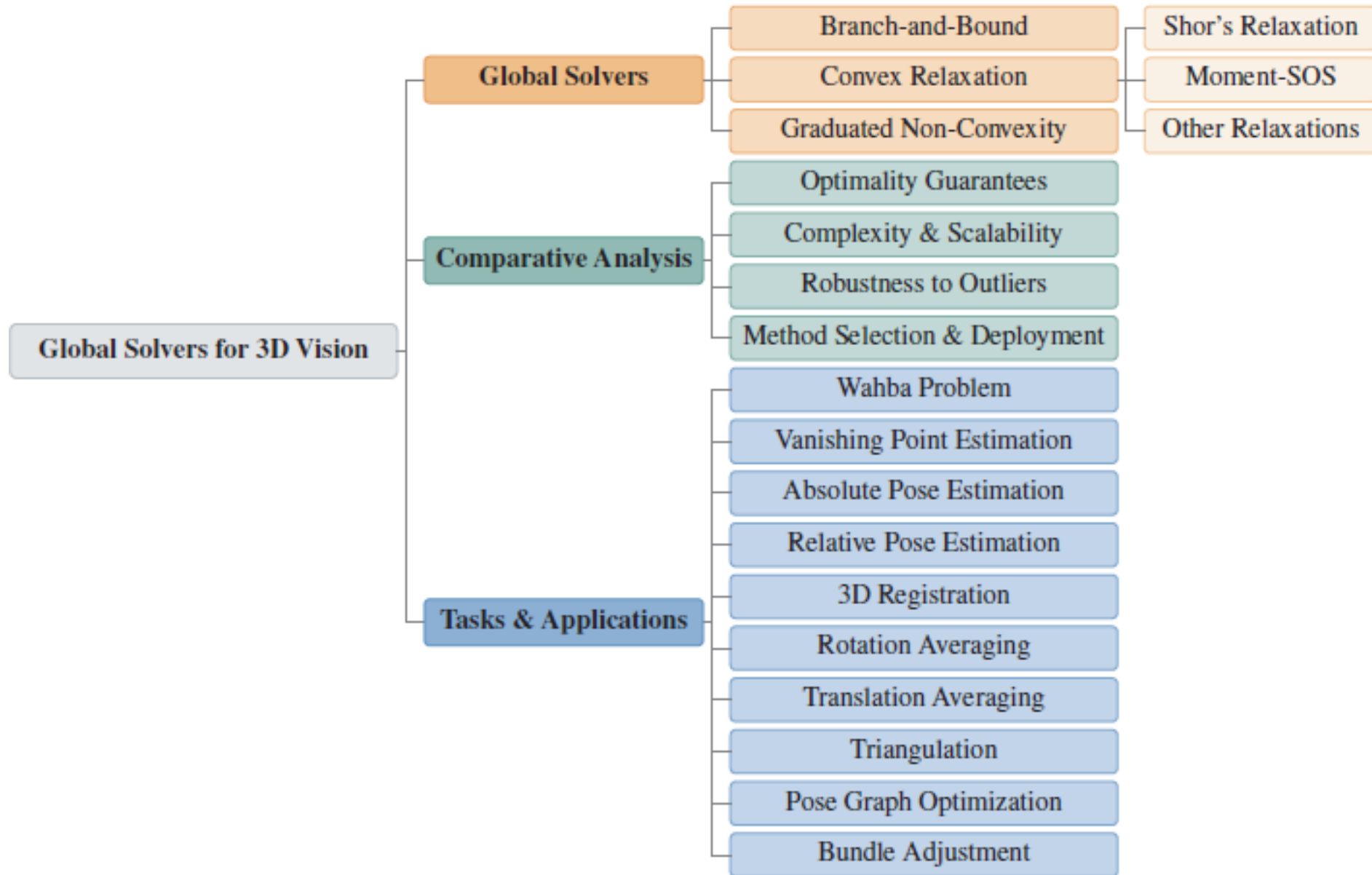
(Seq DW-4)

[1] Song Y, Sohl-Dickstein J, Kingma D P, et al. Score-based generative modeling through stochastic differential equations[J]. arXiv preprint arXiv:2011.13456, 2020.
[2] Akhound-Sadegh T, Rector-Brooks J, Bose A J, et al. Iterated denoising energy matching for sampling from boltzmann densities[J]. arXiv preprint arXiv:2402.06126, 2024.

Advances in Global Solvers for 3D Vision



Overview



Three Paradigm



Branch-and-Bound



Convex Relaxation

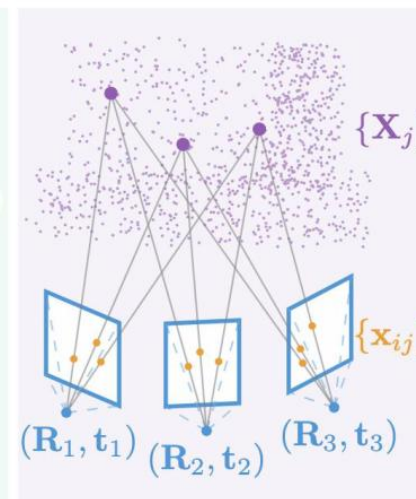
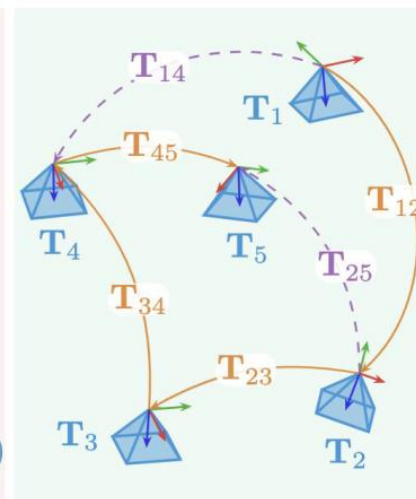
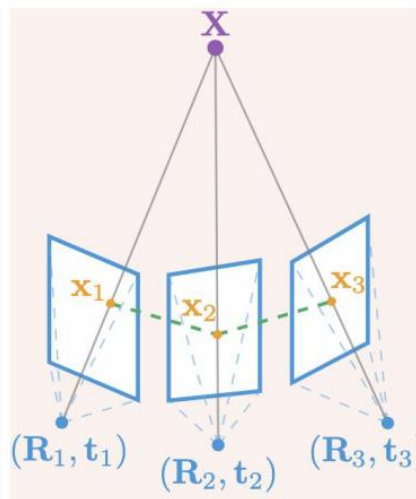
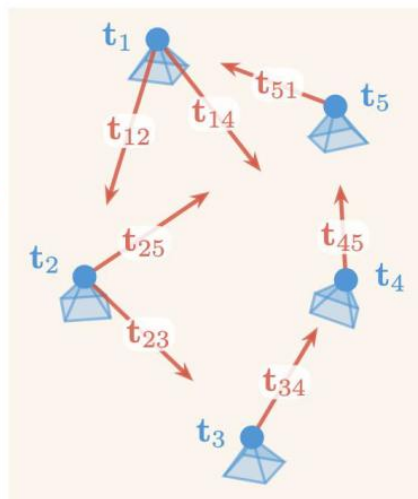
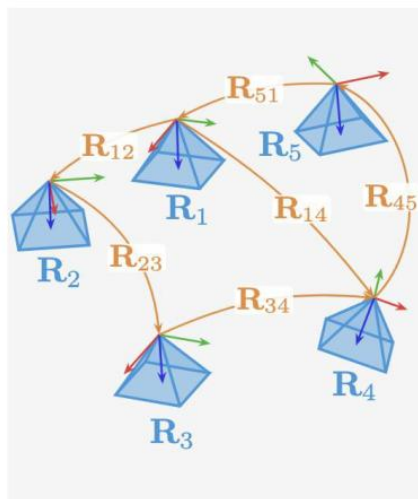
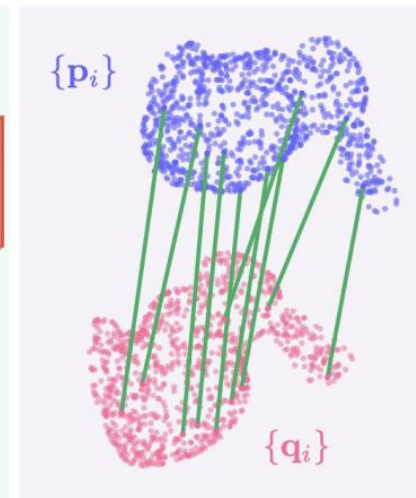
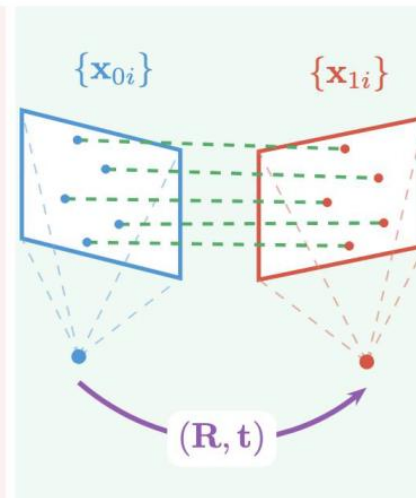
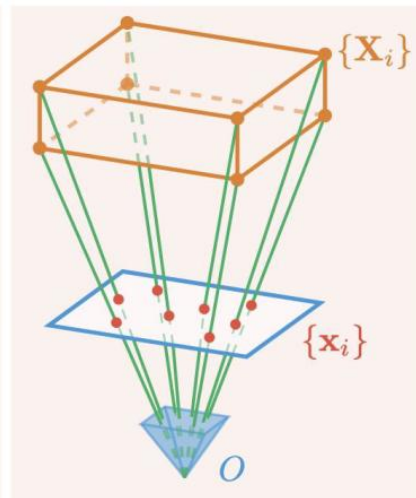
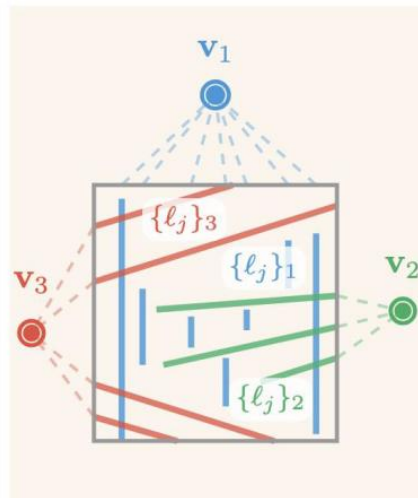
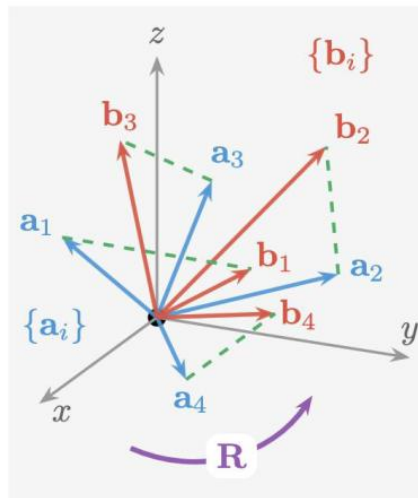


**Graduated
Non-Convexity**

Comparative Analysis

METHOD	OPTIMALITY	SCALABILITY	OUTLIER HANDLING	COMPLEXITY	CERTIFICATES
Branch & Bound BnB	✓ Global	✗ Poor $N < 20$	↗ Consensus Max (CM)	△ Exponential in dim	✓ Always
Shor's Relaxation Convex Relaxation	◆ Global if tight	● Medium 100–1k	→ M-est robust	▷ $O(n^{3.5})$ SDP	◆ If tight
Moment-SOS Lasserre Hierarchy	◆ Global if tight	✗ Low $N < 100$	↗ CM + M-est	△ $O(r^{3.5})$ grows fast	◆ If tight
Other Relaxations L_∞ / SOCP / LP / QP	≈ Near-global prob. spec.	↑↑ High $N > 1k$	● Problem specific	⇒ $O(n^3) \sim O(n)$ fast	● Prob. specific
GNC Grad. Non-Convexity	≈ Near-global no cert.	★ Excellent $N > 1k$	▲ Built-in 30–50%	⇒ $O(Kn^2)$ linear N	✗ None
● Strong ◆ Good / Conditional ● Moderate ● Limited					

Ten Geometric Estimation Problems



1

Motivation: Why Trustworthy Perception?

2

Certifiable Global Optimization

- GlobustVP: Certifiable VP Estimation [CVPR 2025, Best Paper Award Candidate]
- NPC: RL-Accelerated Homotopy Solvers [ICLR 2026]
- Survey of Global Solvers for 3D Vision

3

Open challenges

1

Motivation: Why Trustworthy Perception?

2

Certifiable Global Optimization

- GlobustVP: Certifiable VP Estimation [CVPR 2025, Best Paper Award Candidate]
- NPC: RL-Accelerated Homotopy Solvers [ICLR 2026]
- Survey of Global Solvers for 3D Vision

3

Open challenges

Open Challenges and Future Directions

Scalability

BnB and CR costs grow prohibitively with problem size

Open:

Hybrid pipelines pairing fast GNC with lightweight certifiers

Deep Learning Integration

Foundation models produce impressive predictions without certificates.

Open:

CR as differentiable layers and learned priors to warm-start solvers

Standardized Evaluation

The field lacks shared benchmarks enabling fair comparison.

Open:

Certified optimality rate, tightness gaps, runtime-accuracy curves

Thank You!



Javier Civera



Haoang Li



Heng Yang



Yi Zhou



Peidong Liu



Bangyang Liao



Jiayao Mai



Yingping Zeng



Daniel Cremers



Tailin Wu